
Hyper-Kamiokande Project Status and Plans

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and for Yury Kudenko**

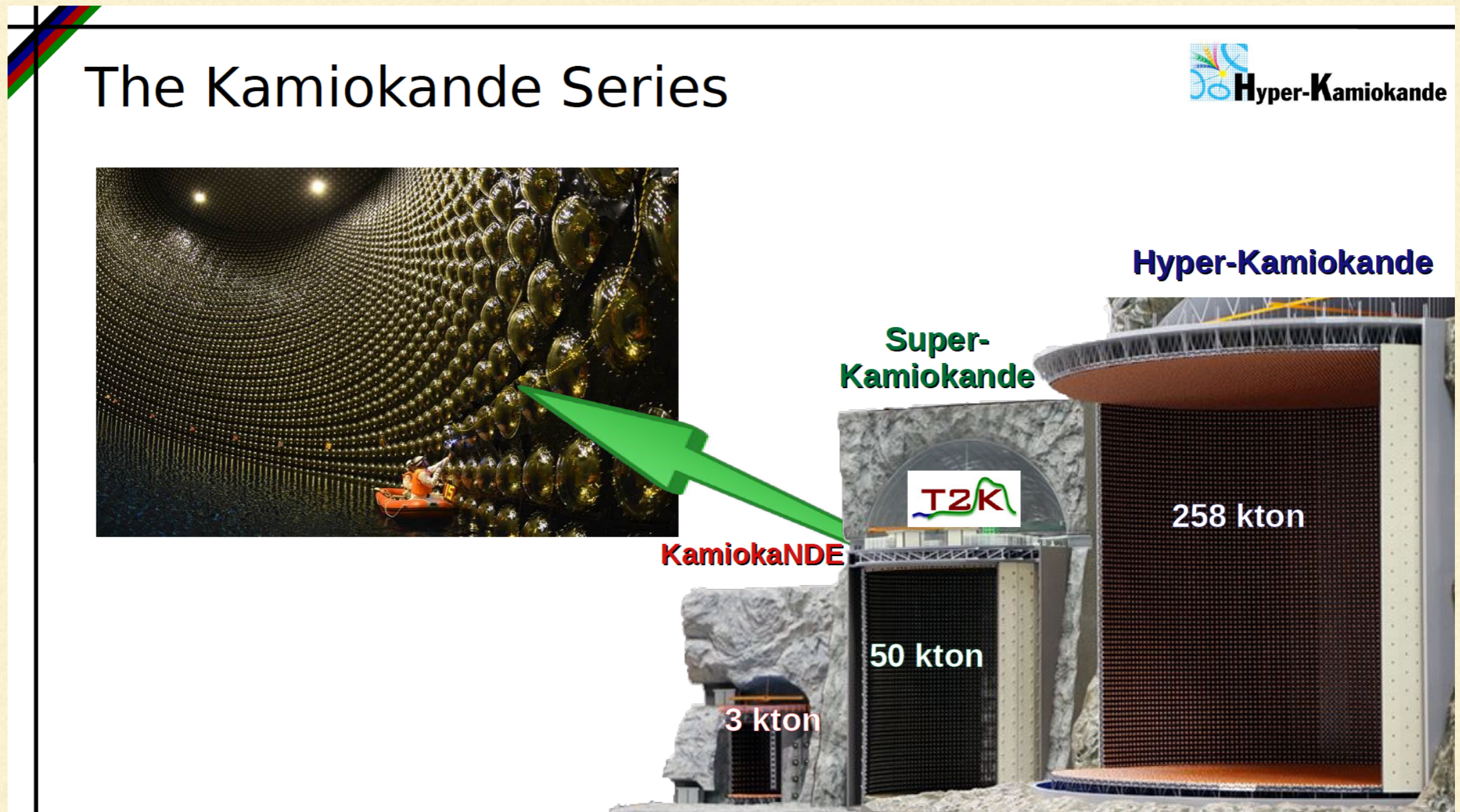
October 5, 2021

Future neutrino projects

- Despite a huge success of the past and current neutrino experiments in fulfilling the neutrino puzzle a range of question exists that requires further efforts
- Neutrino mass ordering, CP-violation in neutrino (lepton) sector, θ_{23} - angle (octant, any new symmetries?), sterile neutrinos?, non-standard interactions?, heavy neutral leptons?
- A new generation of experiments is needed is needed to provide definitive determinations of neutrino properties
 - And accelerator based neutrino beams will continue their one of the leading roles
- Here we enter **Hyper-Kamiokande** and DUNE era

Hyper-Kamiokande detector

- Further superb iterations of the Kamiokande physics



Hyper-Kamiokande detector

- The main idea is to build the new unique large-scale water Cherenkov detector

The Hyper-K Detector
Water Cherenkov detector

Photomultiplier tube (PMT)

APPROVED

Hyper-Kamiokande

The diagram illustrates the detection principle of the Hyper-Kamiokande detector. A neutrino (represented by a small orange sphere) interacts with a charged particle in water (represented by a blue sphere), producing Cherenkov light (represented by a yellow starburst). This light is detected by a PMT (Photomultiplier Tube), which is shown as a large, cylindrical device with a grid of photosensors. A large red stamp reading "APPROVED" is overlaid on the diagram. Below the main diagram, three particle interaction diagrams are shown: Muon, Electron, and π^0 . Each diagram consists of a central rectangular panel with a circular inset above and below it, showing the characteristic ring-like pattern of Cherenkov light produced by the respective particle.

Cherenkov light

Neutrino

Charged particle in water

Photosensors

Muon

Electron

π^0

Hyper-K will begin taking data in 2027

Hyper-Kamiokande detector design

- Inner and outer detectors

The Hyper-K Detector



Inner detector (ID):

* 216 kton

Outer detector (OD):

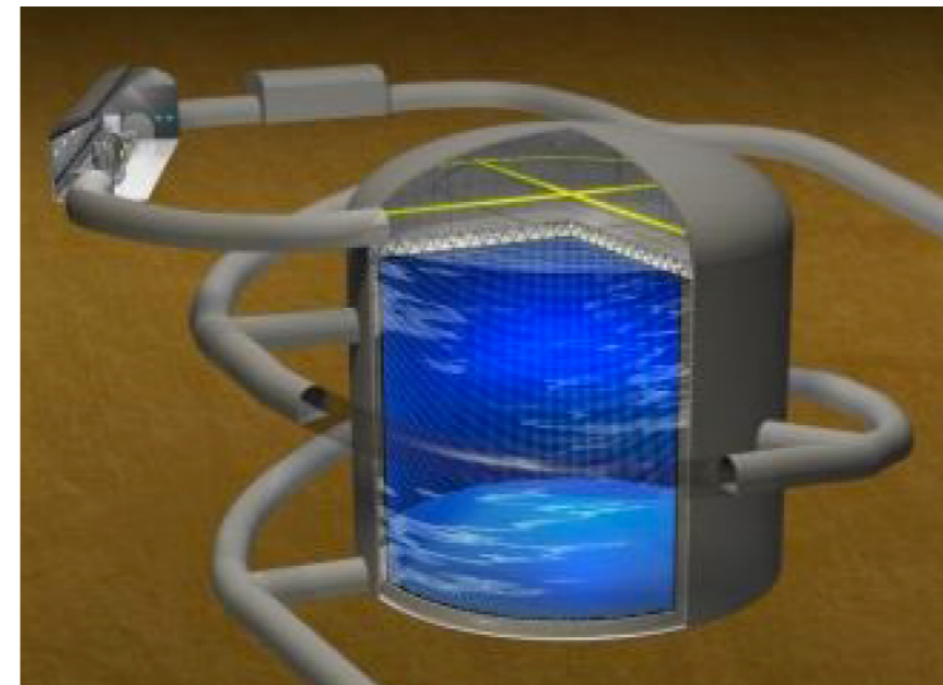
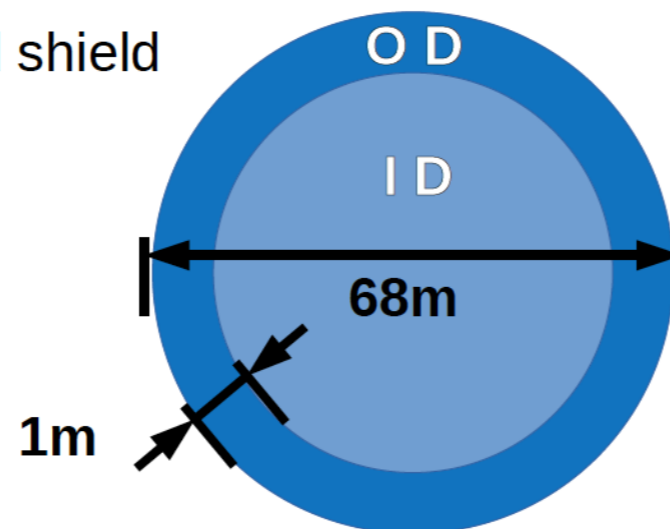
* 1m thick round the edge, 2m at top/bottom

* veto region (incoming/outgoing particles)

* low energy background shield

ID / OD boundary

→ high reflectivity
(>90%) Tyvek



Height = 71m, Diameter = 68m

Volume: 258kton

Hyper-Kamiokande detector design

- PMTs

PMT Photosensors

50cm PMTs (box and line dynode)
~ 1.5 ns timing resolution

Inner detector (ID)

20,000 * 50cm PMTs → 20% coverage



8cm PMTs

Outer detector (OD)

~10,000 * 8cm PMTs



Multi-PMTs (mPMTs)

- 19 x 8cm PMTs inside single pressure vessel

- directional information and improved timing and spatial resolutions

Inner detector (ID)

~ few thousand mPMTs



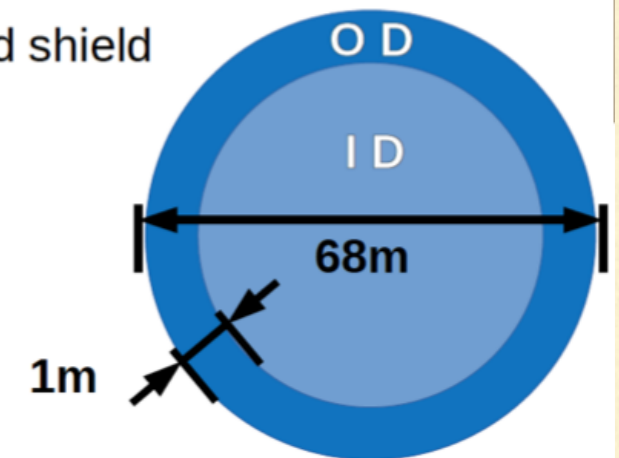
Hyper-Kamiokande Outer Detector INR RAS Efforts

- Relatively thin volume of OD (vs 2.6-2.7 m in SuperK)
- Need high-detection efficiency to achieve and improve physics capabilities
- Need efficient light-collection
- Super-Kamiokande: acrylic bis-MSB doped WS plates with a hole to mount a PMT
 - Absorbing UV light and re-irradiating photons in the blue-green, better matching PMTs spectral sensitivity
- Reviewing and testing the approach for HyperK

Outer detector (OD):

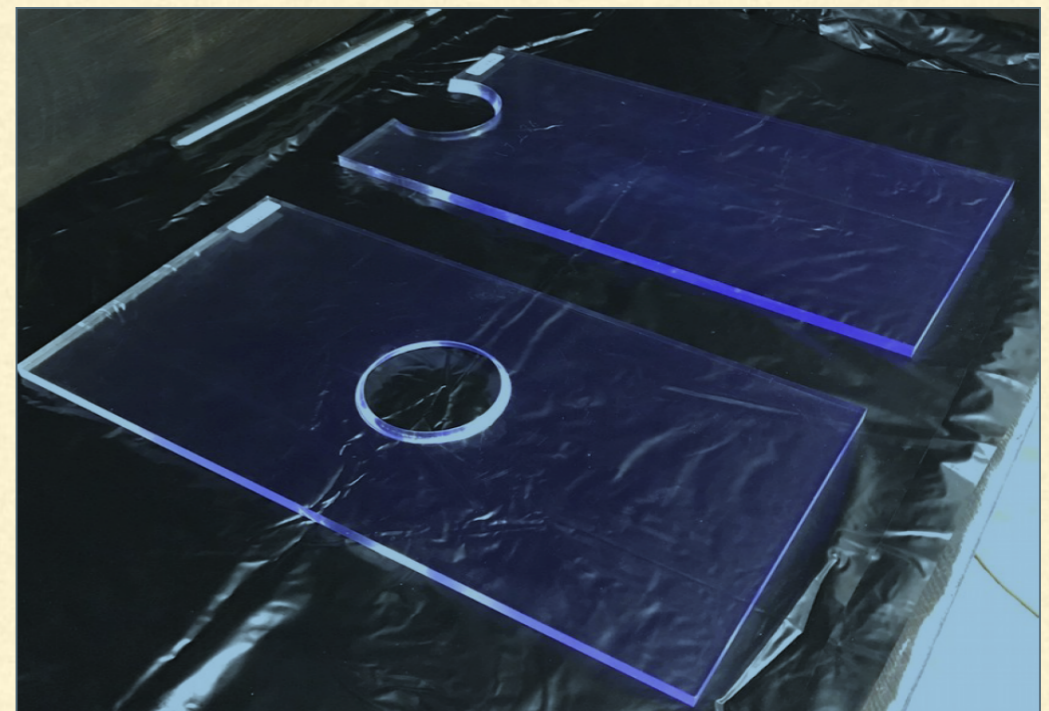
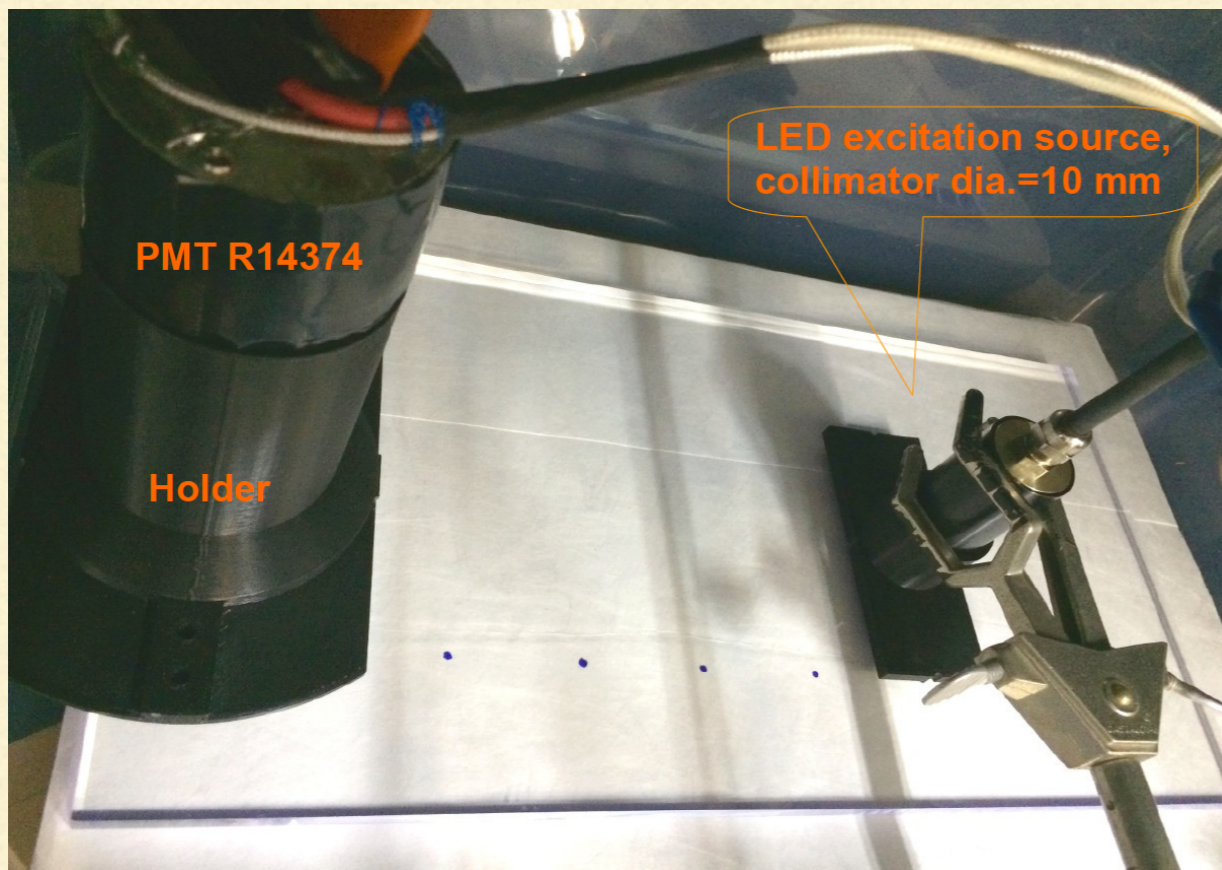
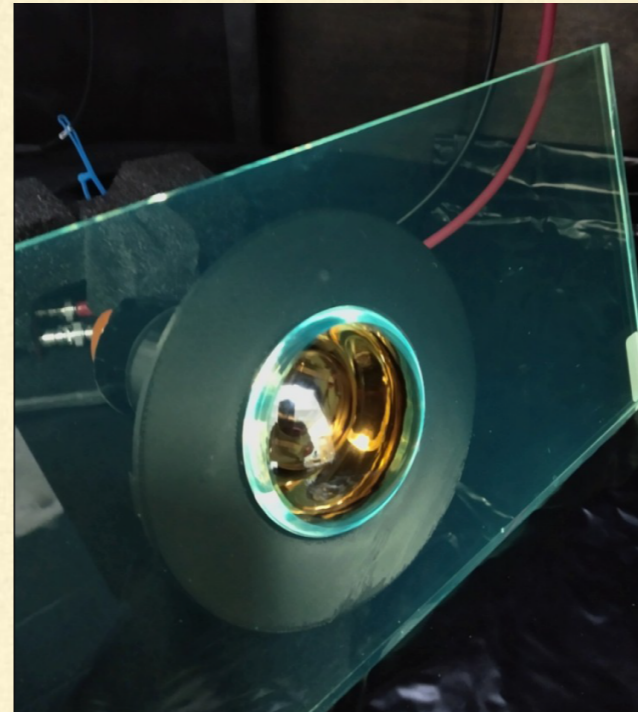
- * 1m thick round the edge, 2m at top/bottom
- * veto region (incoming/outgoing particles)
- * low energy background shield

ID / OD boundary
→ high reflectivity
(>90%) Tyvek



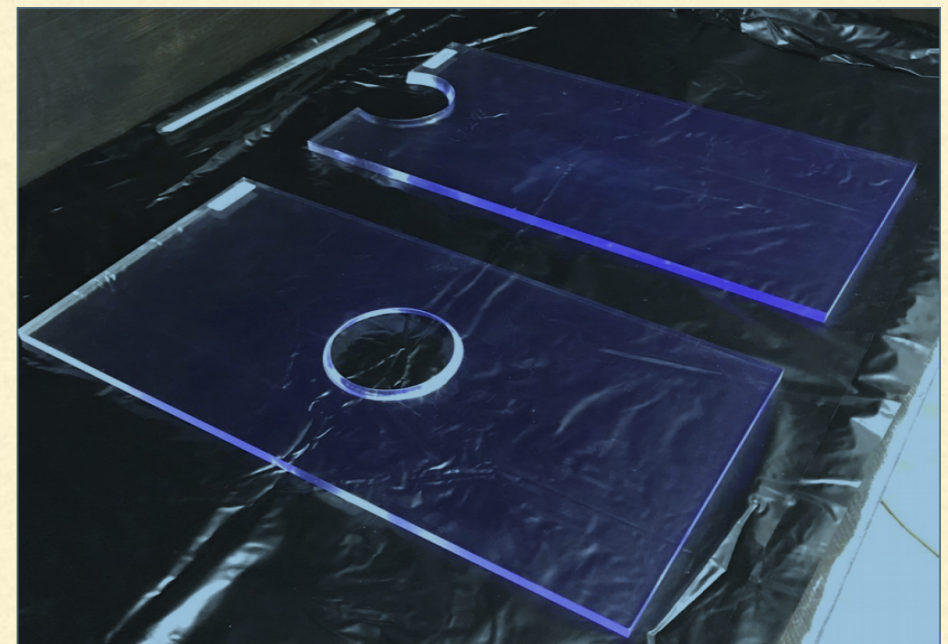
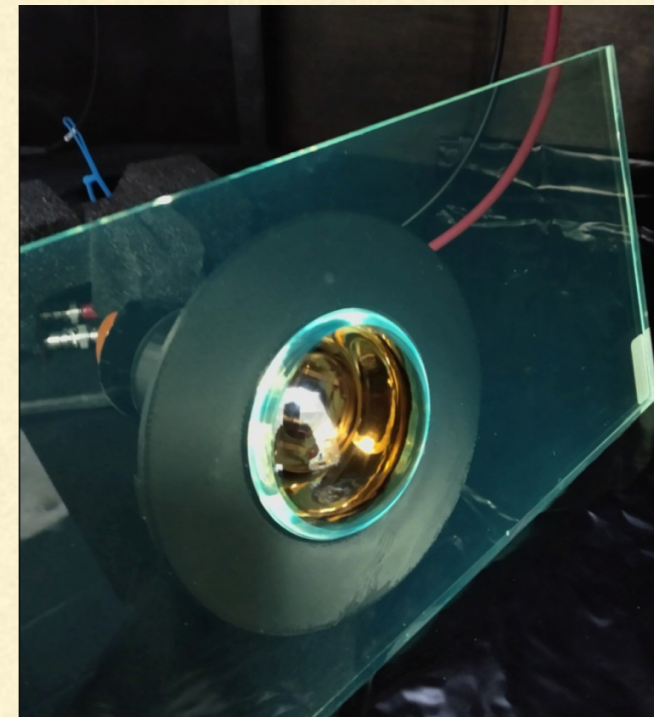
Hyper-Kamiokande Outer Detector PMMA Plates, INR RAS Efforts

- Collaboration with НИИ Полимеров, Dzerjinsk, Russia
- Test different plate compositions and configurations on the light-collecting efficiency



Hyper-Kamiokande Outer Detector PMMA Plates, INR RAS Efforts

- Collaboration with НИИ Полимеров, Dzerjinsk, Russia
- Test different plate compositions and configurations on the light-collecting efficiency
- POPOP(200) doped PMMA plates tested with an INR test-bench
- Up-to 75% increase in light collection efficiency gained with the WLS plates
 - More tests on-going



Hyper-Kamiokande physics program

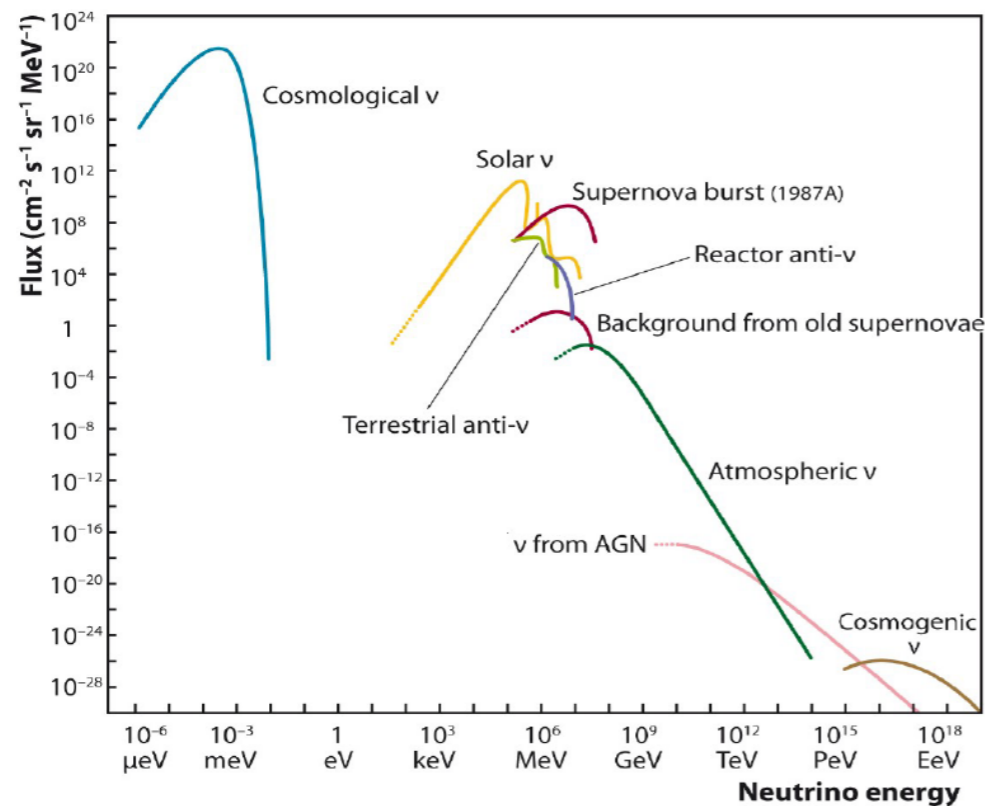
- Wide opportunities for studies

The Kamiokande Series

- * Proton decay
- * Solar, supernova and atmospheric neutrinos
- * Accelerator beam neutrinos



Hyper-Kamiokande



Hyper-Kamiokande physics program

- Wide opportunities for studies

Hyper-Kamiokande Physics



* Neutrino Oscillations

- beam, atmospheric, solar neutrinos
- BSM (sterile searches, non-standard interactions etc.)

* Astrophysics

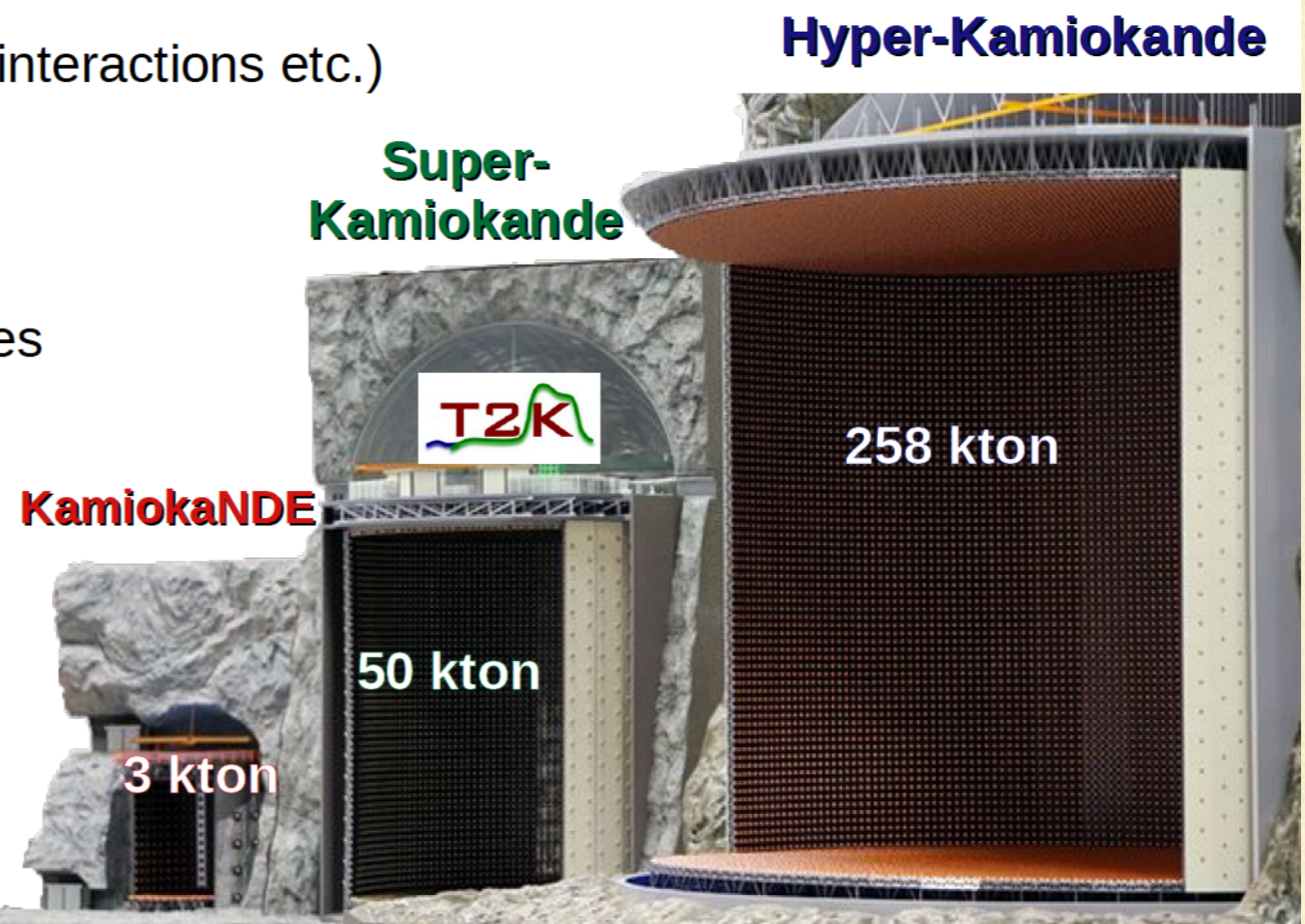
- solar neutrinos, supernova neutrinos
- dark matter, gravitational-wave sources
- gamma-ray sources

* Nuclear physics

- neutrino interactions

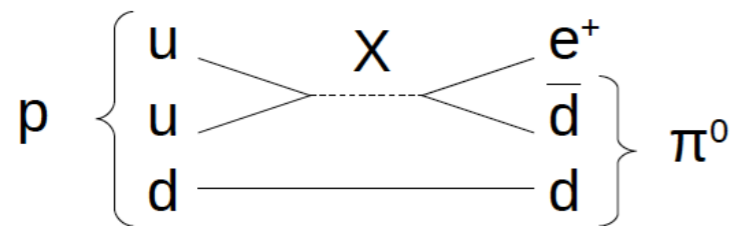
* Geophysics

- matter effect on oscillations
- electron density of Earth's outer core



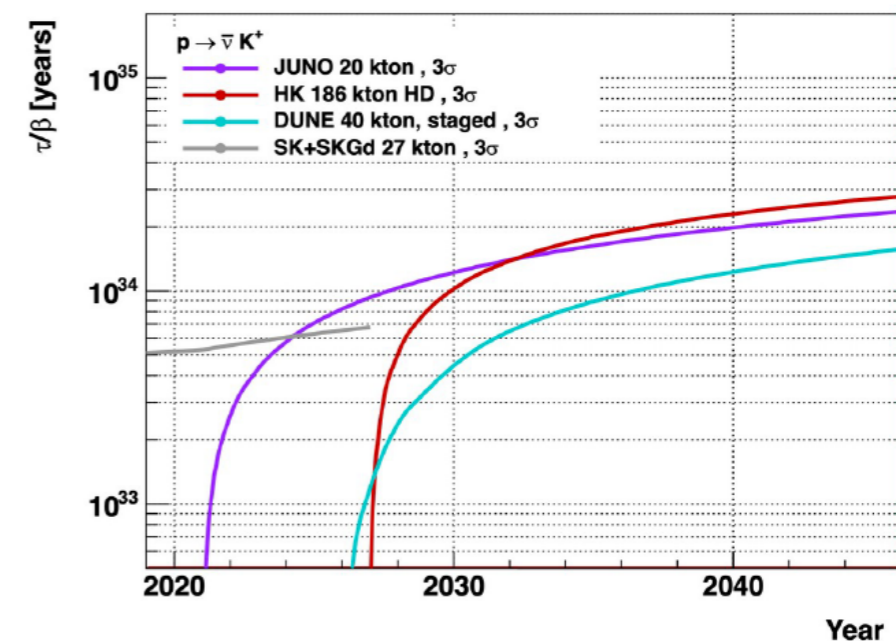
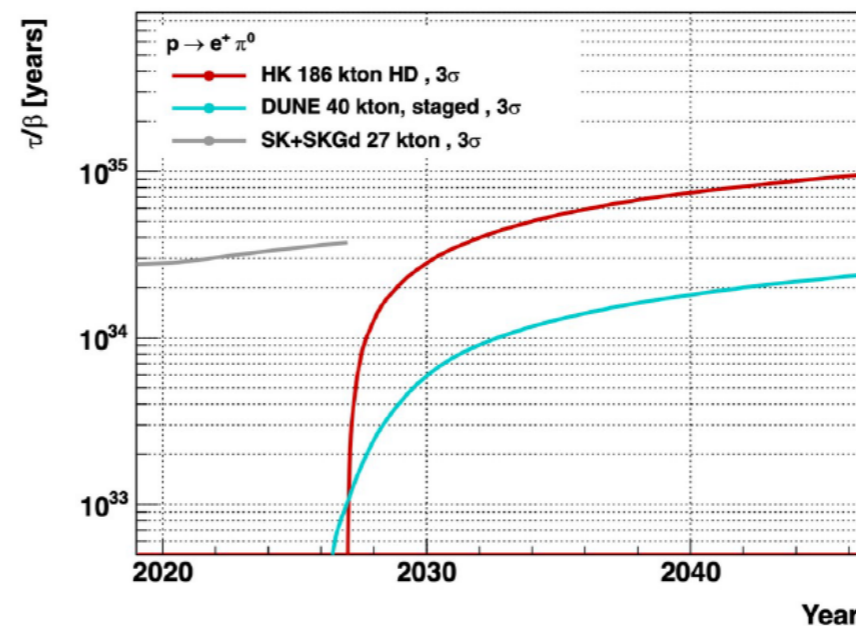
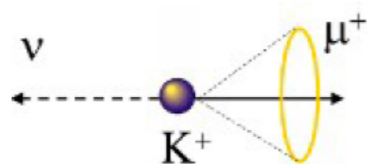
Hyper-Kamiokande: Proton Decay

Proton decay



HK can improve the SK limit on this process from 10^{34} to 10^{35} years

HK also competitive for $p \rightarrow K^+ \nu$



Hyper-Kamikande: Neutrino Oscillations



Neutrino Oscillations

- * Mass and flavour states do not align
- * Non-zero masses
- neutrino osc. governed by PMNS matrix

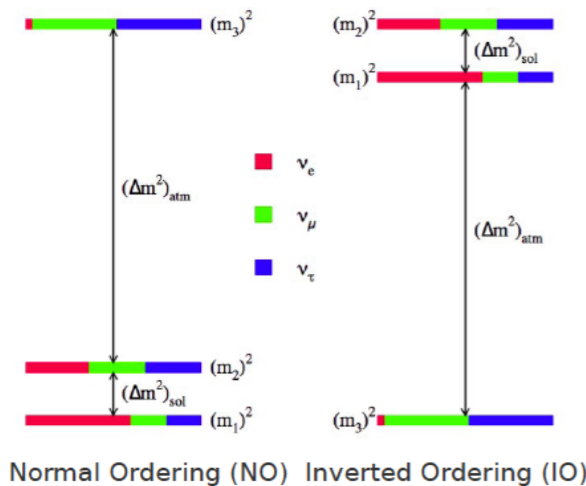
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Atmospheric and
accelerator
 $\theta_{23} \sim 50^\circ$
 $|\Delta m_{32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$

Reactor and accelerator
 $\theta_{13} \sim 8^\circ$
Accelerator only $\delta_{CP} = ??$

Solar and
reactor
 $\theta_{12} \sim 34^\circ$
 $\Delta m_{12}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$

1) Mass Ordering (NO or IO)



2) θ_{23} octant:

$$\theta_{23} > \pi/4 \quad \text{or} \quad \theta_{23} < \pi/4$$

3) CP violation ($\delta_{CP} \neq 0, \pm\pi$)

θ_{13} precisely measured and not too small
→ opens the door for δ_{CP} measurements

If $\delta_{CP} \neq 0, \pm\pi$ → **CP violation**: $P(\nu_\mu \rightarrow \nu_e) \neq P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$

Compare oscillation of ν and $\bar{\nu}$ to probe δ_{CP}

Matter effects! (electrons)

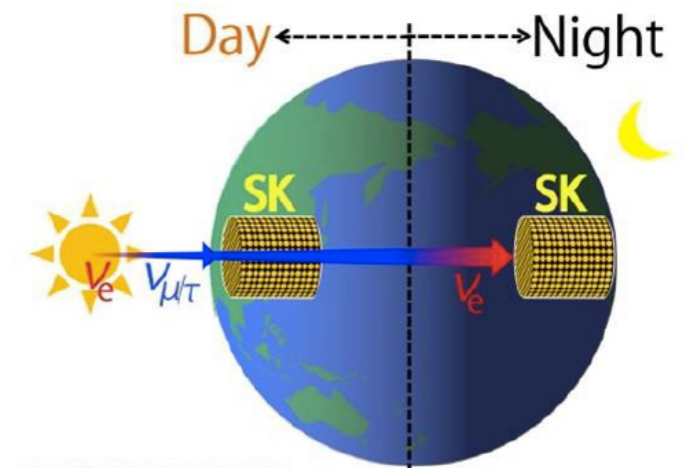
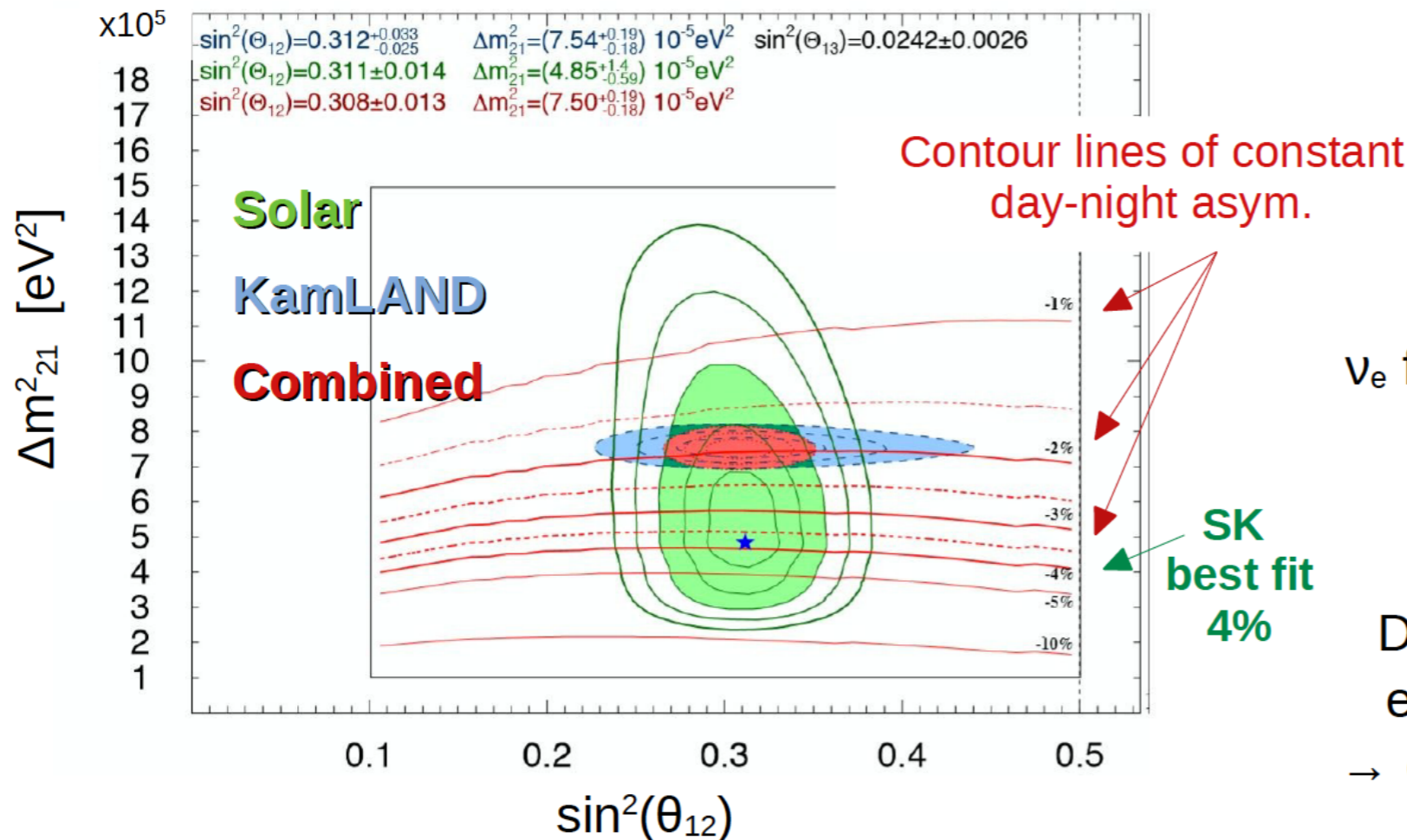
Difference in ν_e and $\bar{\nu}_e$ travelling through the earth (similar effect as δ_{CP})
→ allows for mass hierarchy determination

Hyper-Kamikande: Solar Neutrinos



Solar Neutrinos

~ 2σ tension in Δm_{21}^2 between solar & kamLAND (reactor)



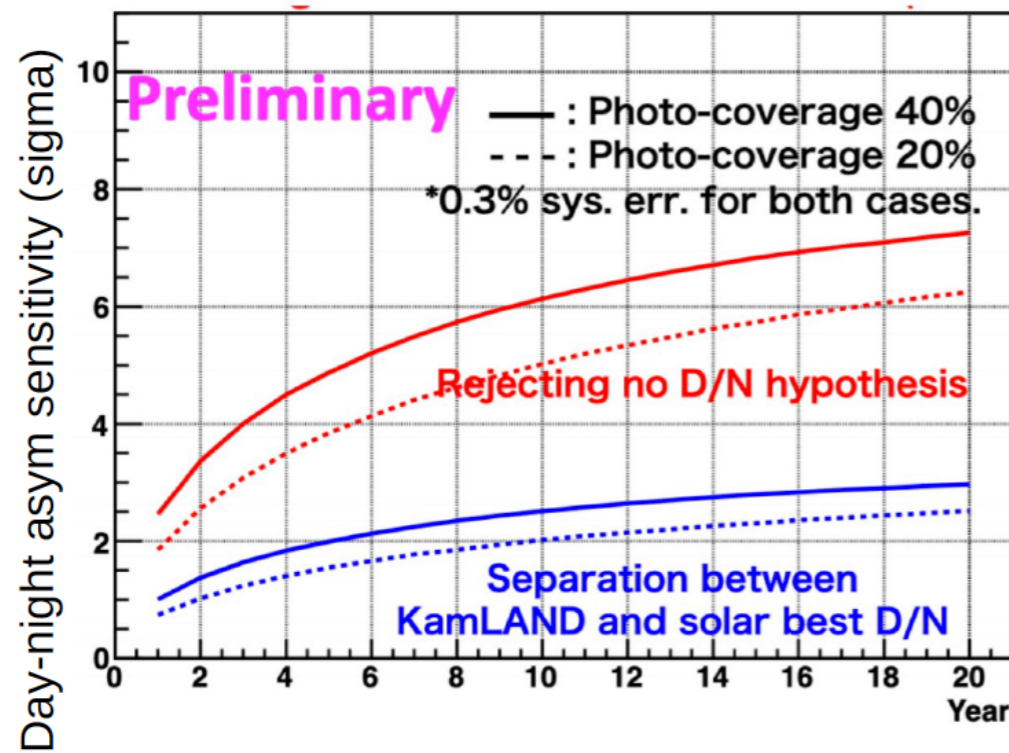
ν_e flux differs between night and day
 → matter effects
 → *day-night asymmetry*

Day-night asymmetry higher than expected from reactor constraint
 → contributes to the Δm_{21}^2 tension

Hyper-Kamikande: Solar Neutrinos

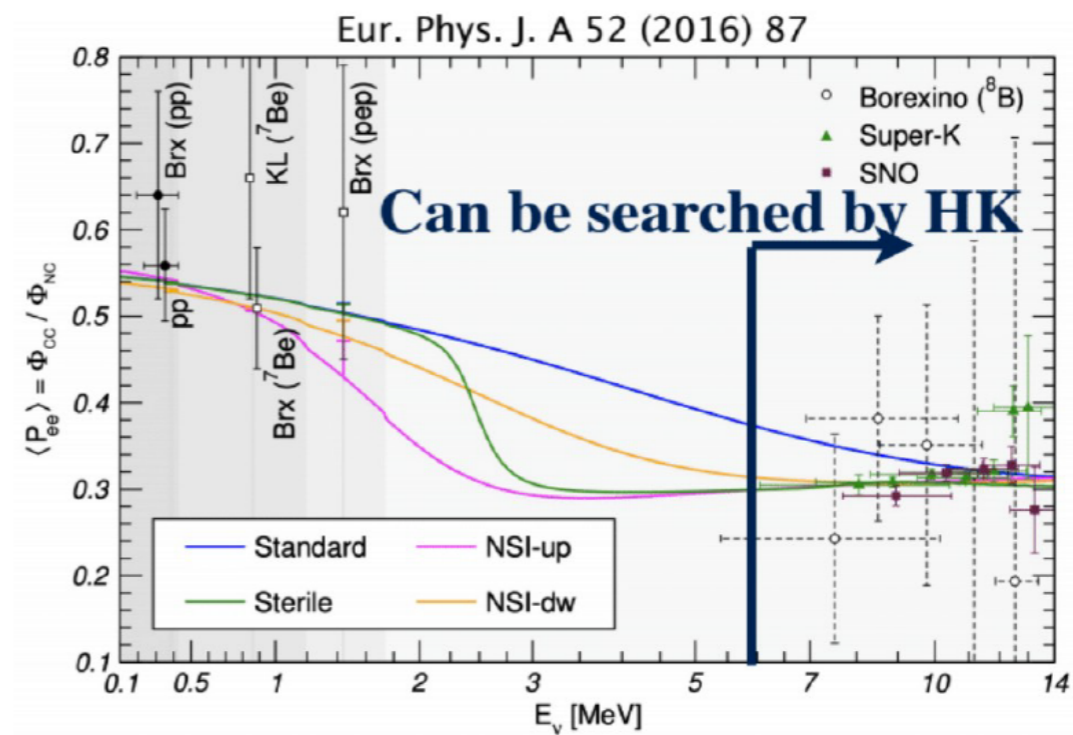
Solar Neutrinos

Hyper-K can constrain the **Day-Night Asymmetry** (and improve Δm^2_{21} tension)



For large D-N asymmetry, expect $>5\sigma$ confirmation 10 years

Hyper-K can constrain the **'upturn'** in the vacuum-MSW transition region in the low energy solar neutrino **survival probability**



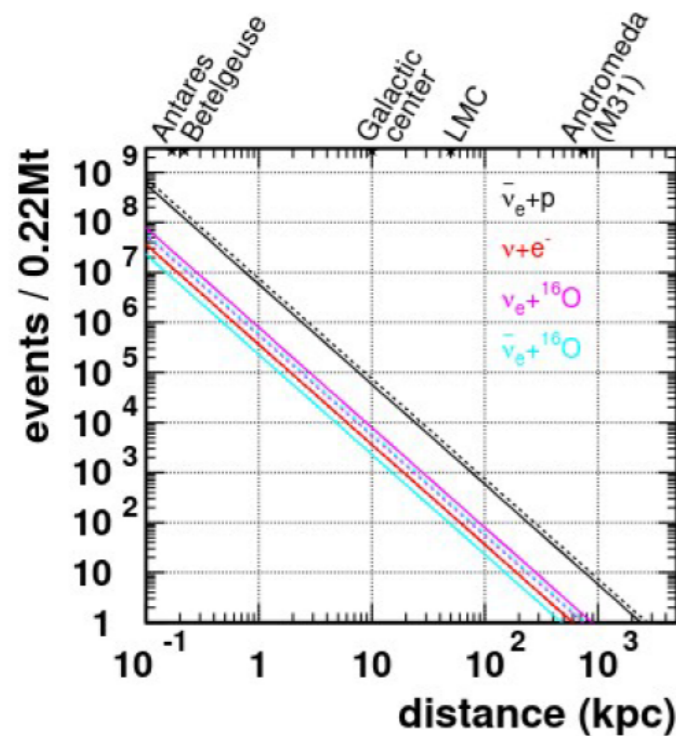
Expect $3-5\sigma$ for upturn discovery after 10 years

Hyper-Kamikande: Supernova Neutrinos



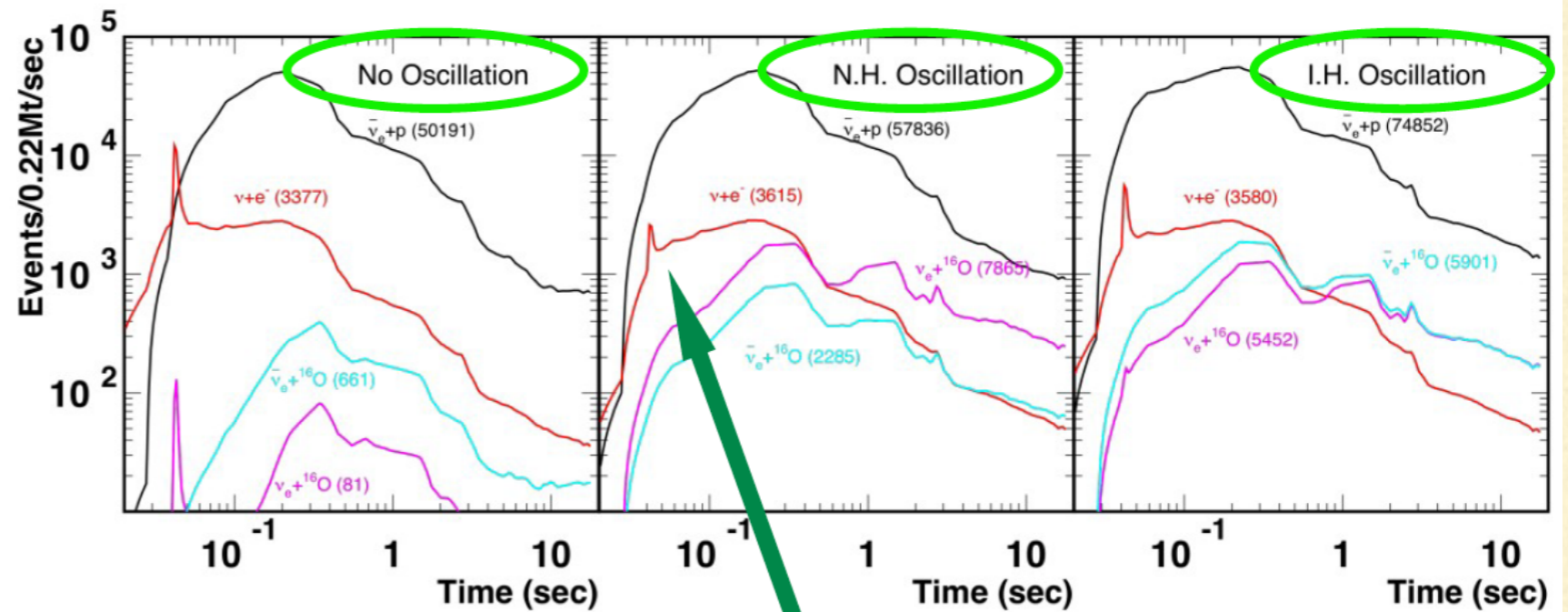
Supernova Neutrinos

Expected number of events as a function of supernova distance



Expected time profile of a supernova at 10kpc

- numbers in brackets total interactions integrated over the 10s burst
- peak event rate of inverse beta decay events (black) reaches ~50 kHz



Neutronization peak
(sensitive to mass ordering)

Supernova Model Discrimination with Hyper-Kamiokande

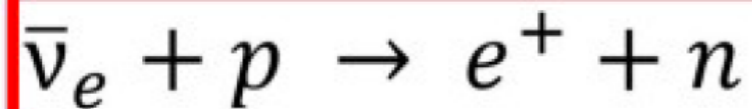
K. Abe et al 2021 ApJ916 15

<https://arxiv.org/abs/2101.05269>

Hyper-Kamikande: Supernova Neutrinos

Supernova Neutrinos

Inverse beta decay dominates



Different models predict different electron antineutrino rates

→ Hyper-K can constrain different models

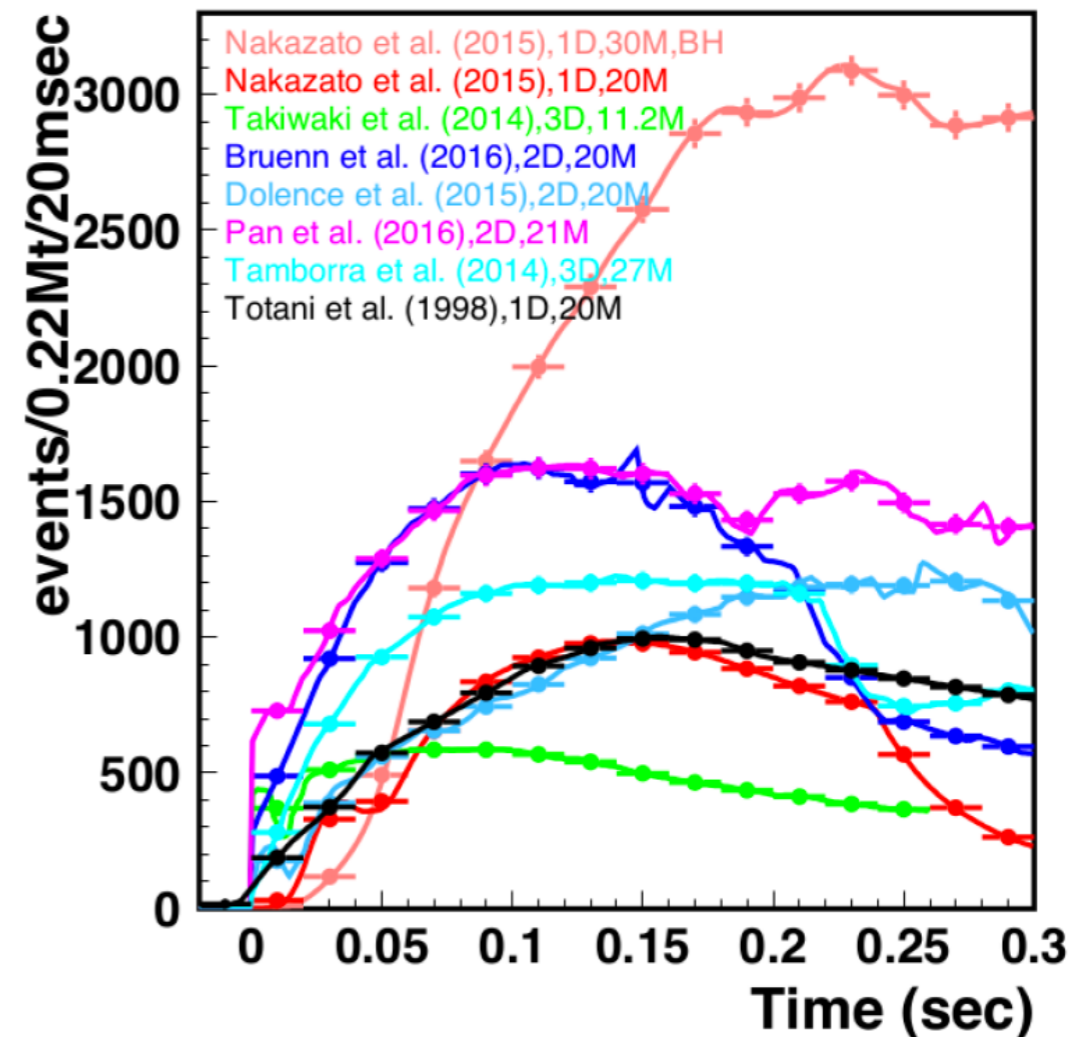
* Stat error is much smaller than the difference between models

* Neutrino detection threshold of 3 MeV

* Directional reconstruction allows for event-by-event measurement



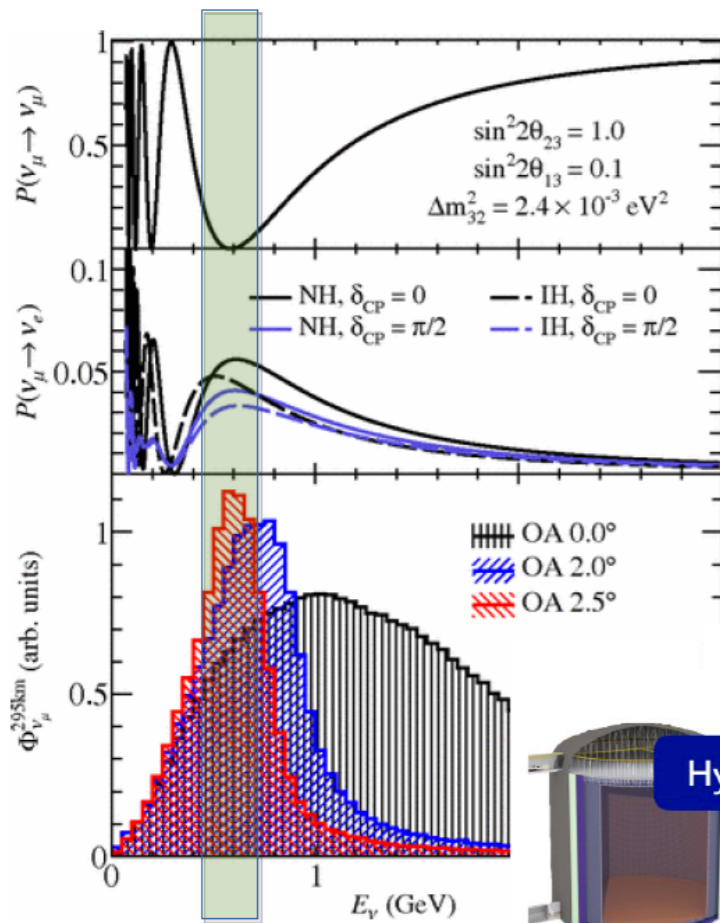
Predicted inverse beta decay rates



Hyper-Kamikande: Long-baseline neutrino interactions (beam)

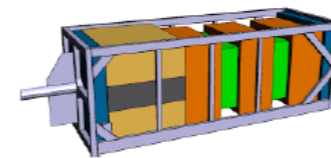


Hyper-Kamiokande long-baseline



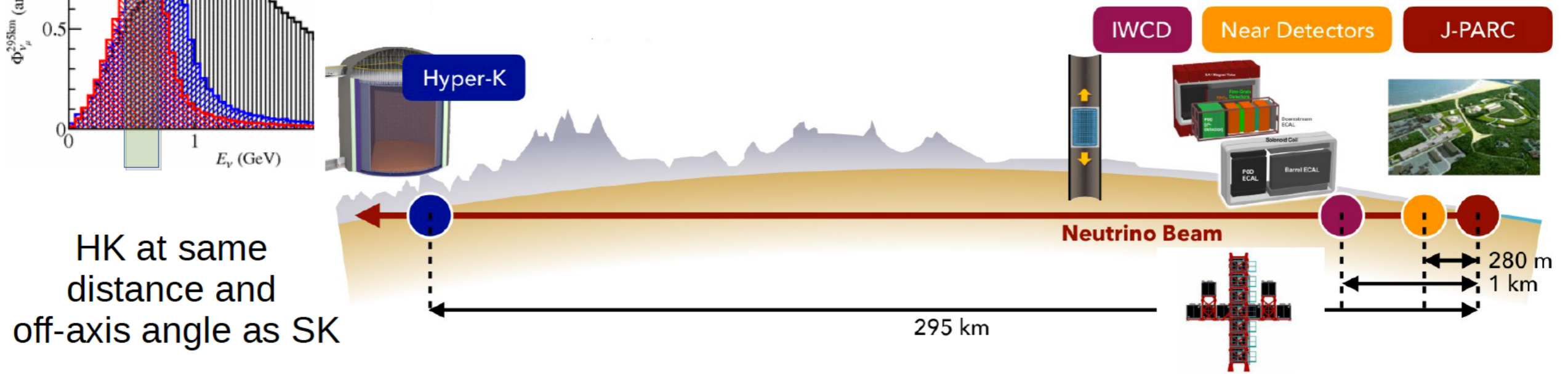
* Upgrade T2K beam to 1.3MW

* Upgraded ND280



* New intermediate water Cherenkov detector (IWCD)

* Hyper-K far detector

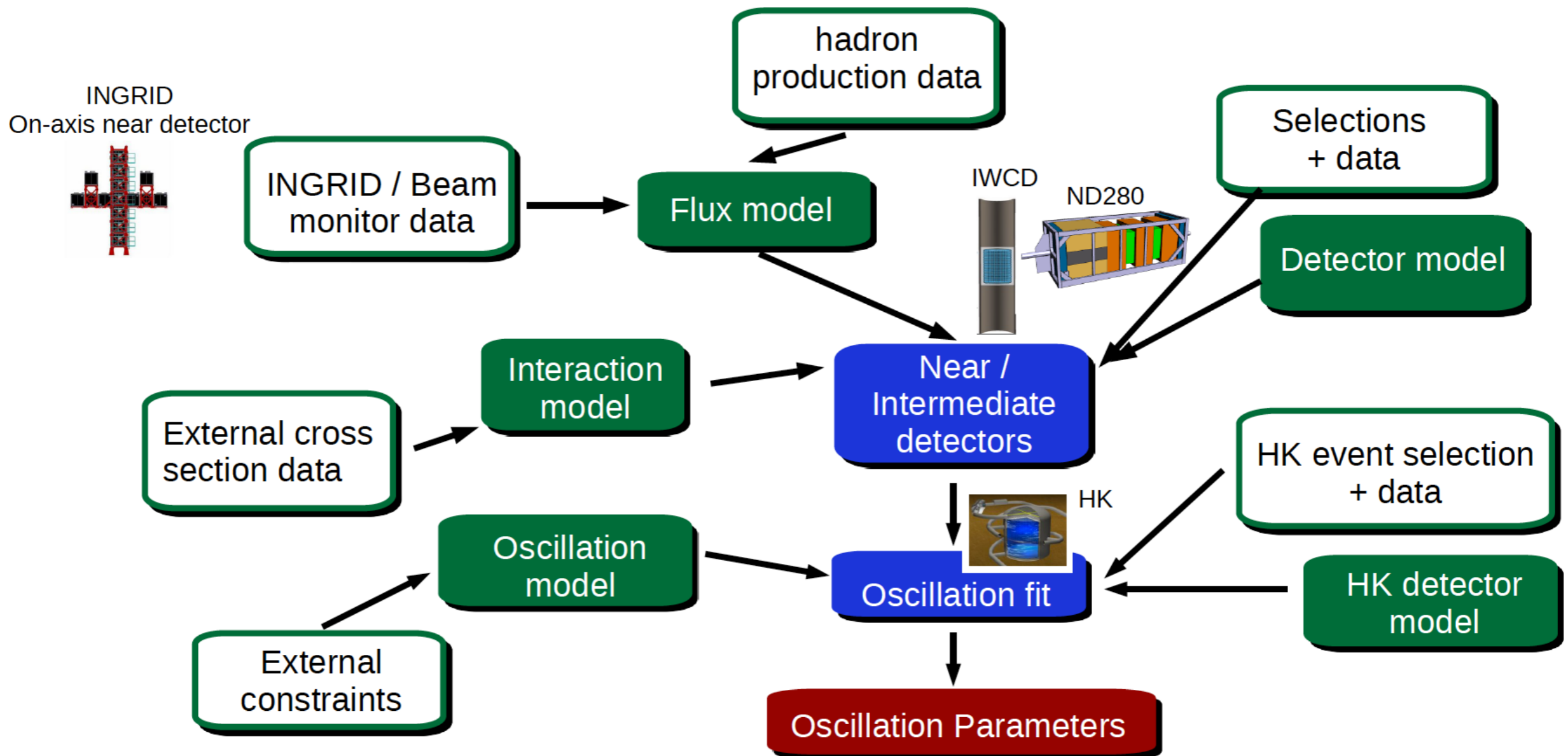


HK at same distance and off-axis angle as SK

Hyper-Kamiokande: Long-baseline neutrino interactions (beam)



Hyper-Kamiokande long-baseline

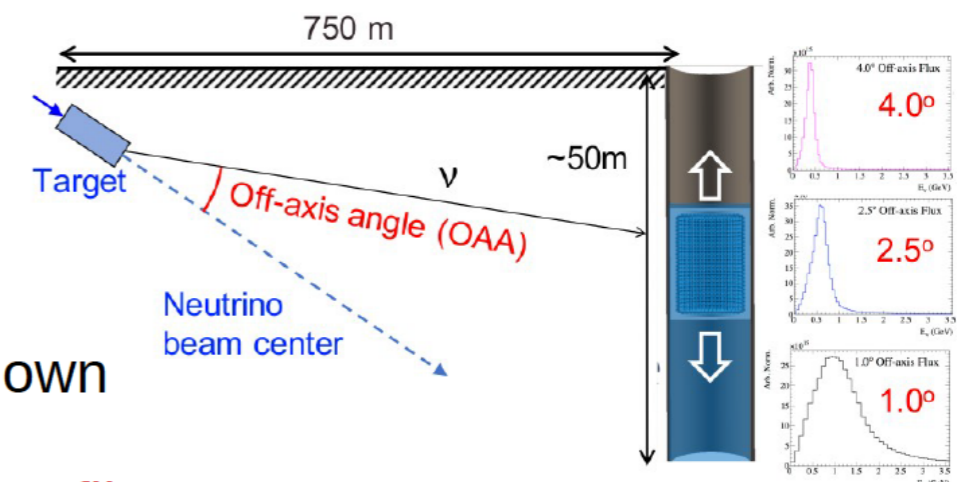


Hyper-Kamikande: Long-baseline neutrino interactions (beam)

Intermediate water Cherenkov detector (IWCD)

Constrain flux and neutrino interactions, with same target as far detector

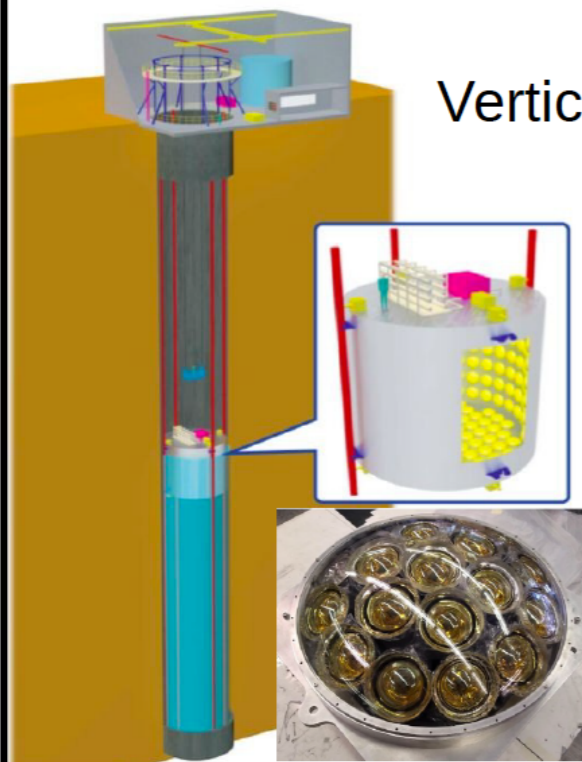
Distance ~ 1km, Diameter ~8m, height ~6m
Size optimised to contain 1GeV muons,
while minimizing beam pile up events



Vertical pit (50m), detector **moves** up and down
→ samples **flux at different angles**
→ sample flux at **different energy profiles**

Multi-PMTs: better **timing** and **spatial** resolution than 1 large PMT
→ good **reconstruction** despite small detector

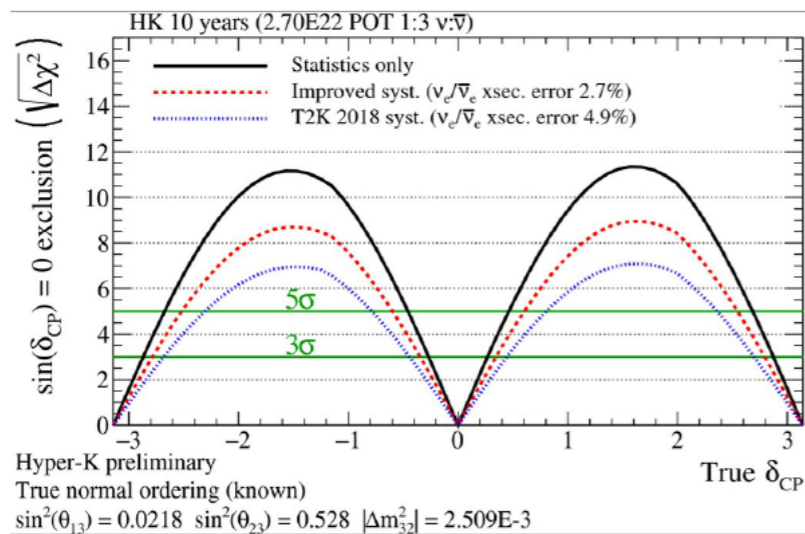
Plans to load with Gadolinium: 0.1% Gd
→ Neutron tagging



Hyper-Kamikande: Long-baseline neutrino interactions (beam)



Hyper-Kamikande long-baseline

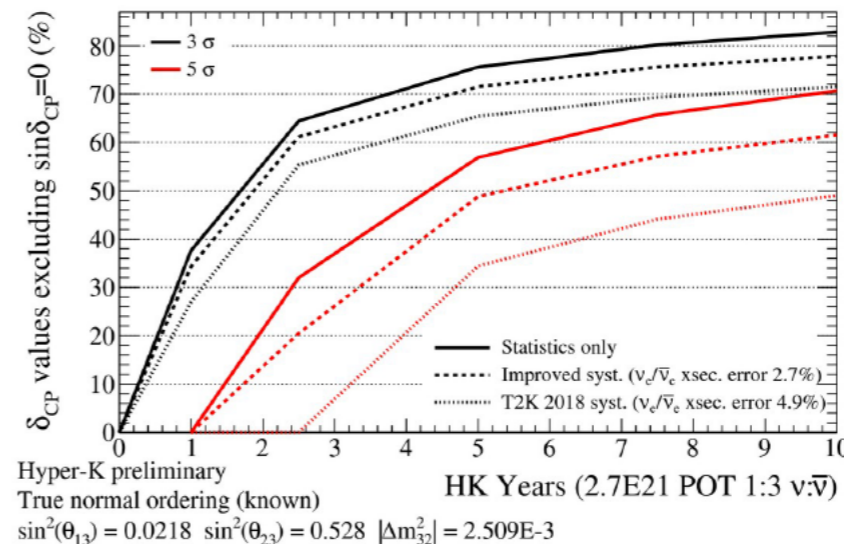


Sensitivity for excluding $\delta_{CP}=0$ given different true values of δ_{CP}

- * Solid line: Statistical errors
- * Small dash: T2K systematic uncertainties
- * large dash: Improved systematic for the $\nu_e/\bar{\nu}_e$ cross section error

The systematic uncertainty on the $\nu_e/\bar{\nu}_e$ cross section will have the largest impact on δ_{CP}
 → Near/intermediate detectors will play a vital role in constraining these errors

5 σ achieved for ~60% fraction of δ_{CP} values with 10years data taking



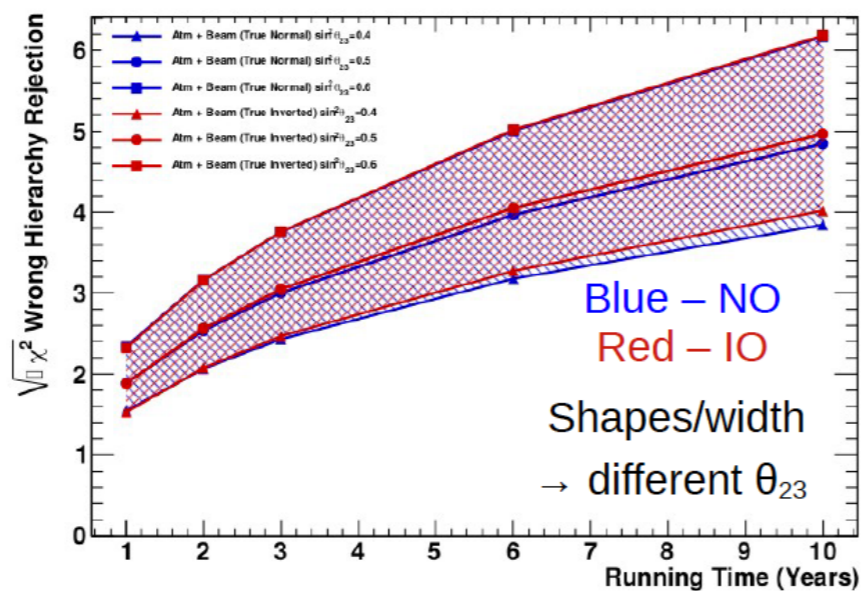
Percentage of true δ_{CP} values for which $\sin(\delta_{CP})=0$ can be excluded, as a function of HK years.

Hyper-Kamikande: Long-baseline neutrino interactions, beam + atmospheric

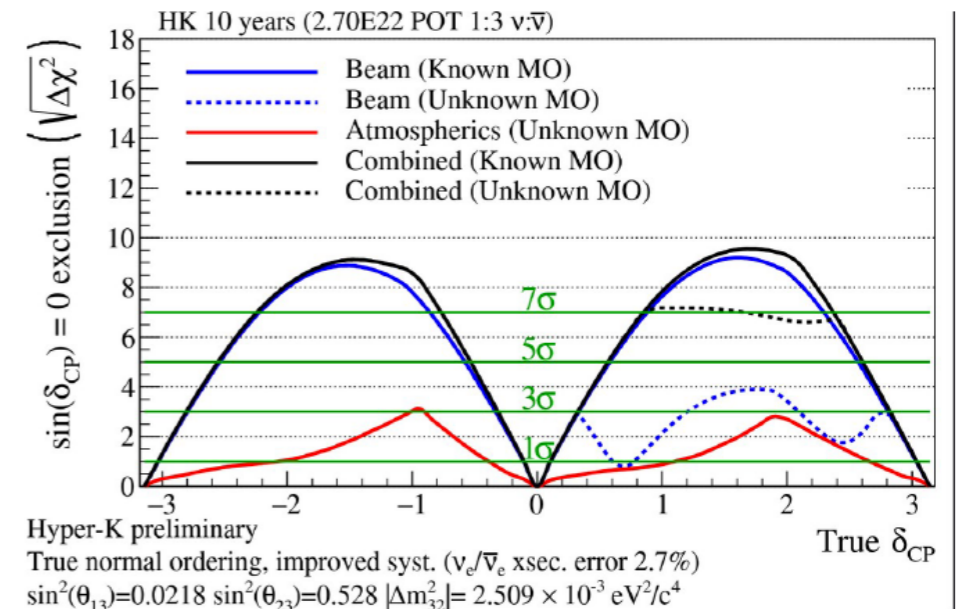


Atmospheric neutrinos + beam

Sensitivity to mass ordering



Sensitivity to CP-violation



Atmospheric neutrinos sensitive to matter effects as they traverse the Earth
 → Sensitive to mass ordering, also helps with θ_{23} octant

Best sensitivity to mass ordering from **combined fit: atmospheric data + beam data**

If mass ordering unknown, atmospheric data improves beam sensitivity to δ_{CP}

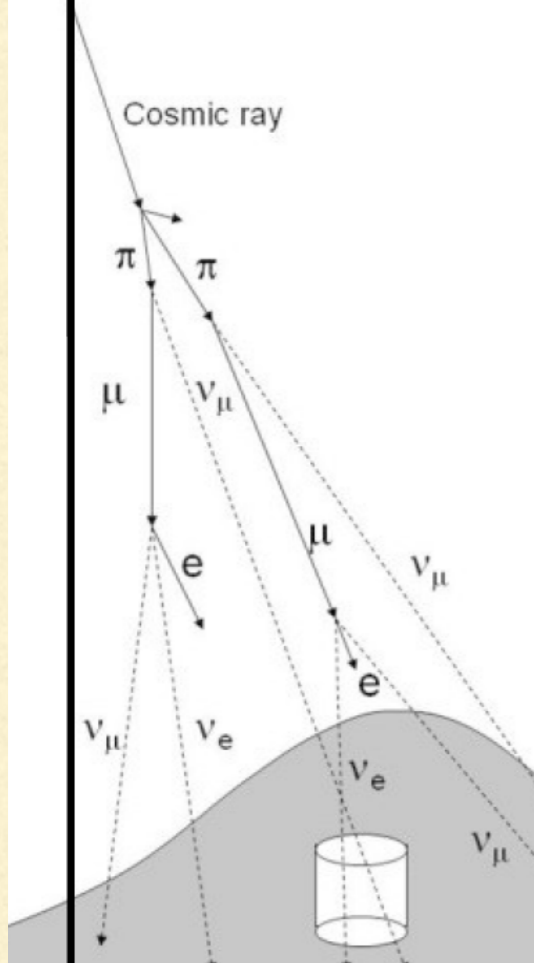


Diagram: Kajita T. (10.2183/pjab.86.303)

Hyper-Kamiokande, stay tuned!

Construction has begun!



UNDER CONSTRUCTION

UNDER CONSTRUCTION

UNDER CONSTRUCTION



ハイパーカミオカンデ 着工記念式典

Hyper-Kamiokande Groundbreaking Ceremony



宇宙線研

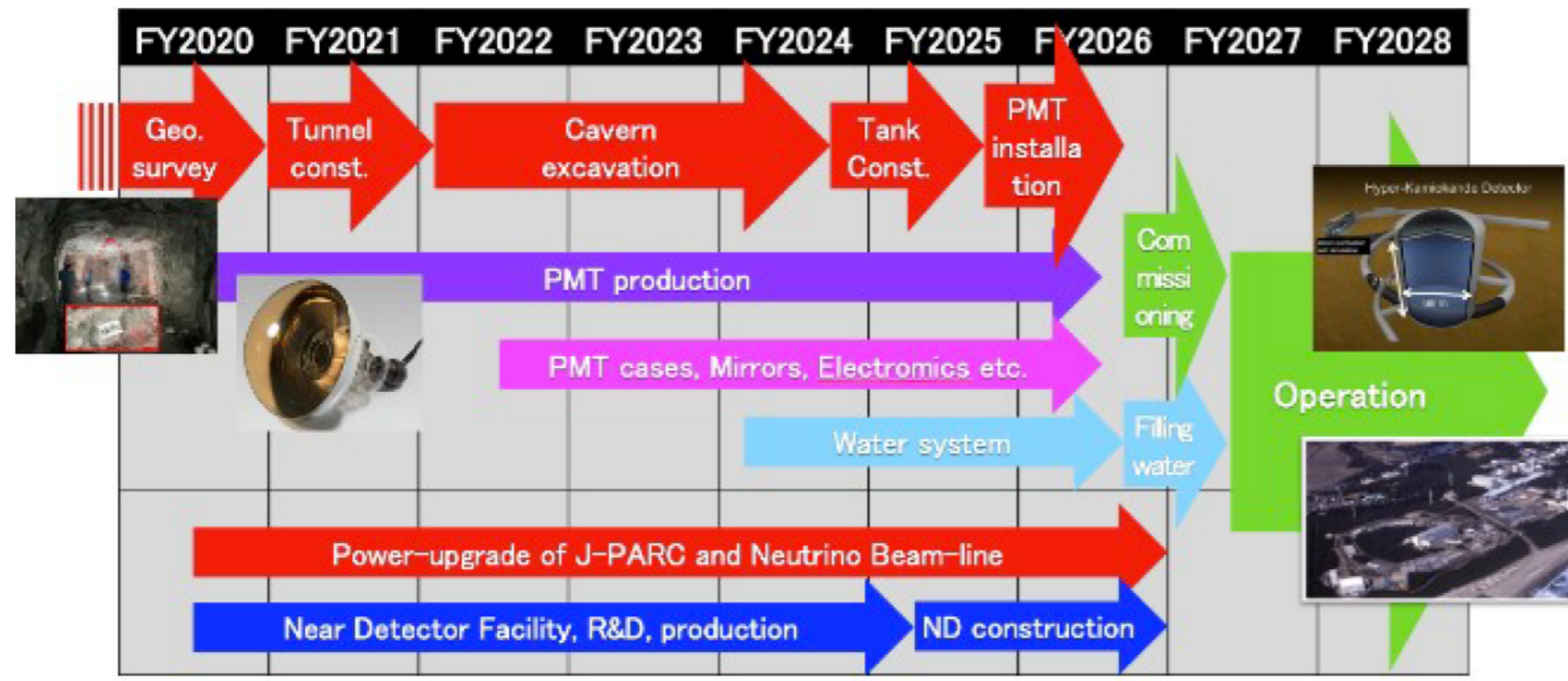
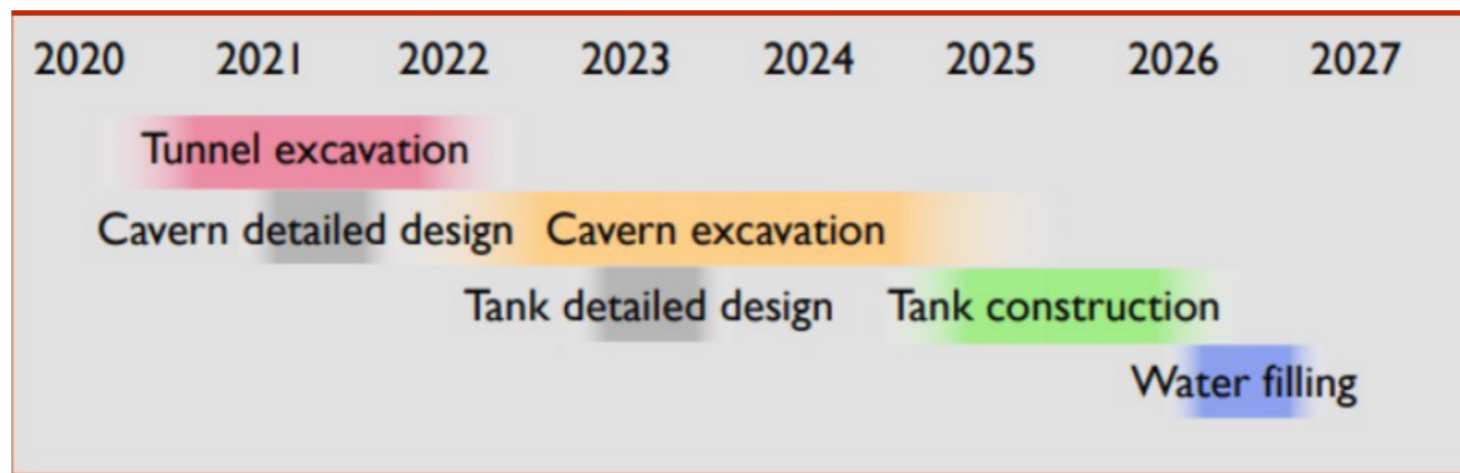
©Institute for Cosmic Ray Research, The University of Tokyo

UNDER CONSTRUCTION

UNDER CONSTRUCTION

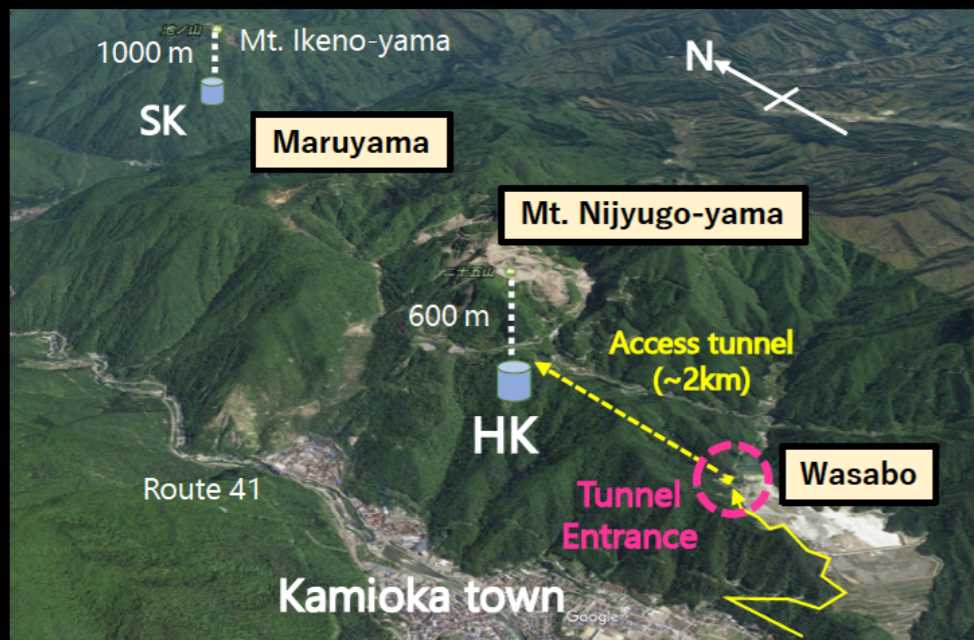
UNDER CONSTRUCTION

Hyper-Kamiokande, stay tuned!



Hyper-Kamiokande, stay tuned!

Entrance Yard Construction



- 👁️ Construction of entrance yard in Wasabo is completed.
- 👁️ Construction of the waste water treatment facility at the entrance yard.



Hyper-Kamiokande, stay tuned!

Access Tunnel Excavation has Started!



- 👁️ Cavern excavation started in May 2021
- 👁️ Groundbreaking ceremony on May 28 2021
- 👁️ Blasting started. Day/night excavation started



Summary



Summary

The Hyper-Kamiokande is a next-generation neutrino experiment

- * Builds on the expertise and knowledge gained from the successful Super-K programme
 - Fiducial volume 8 times larger than SK
 - Improved photosensors
 - beam upgrade to 1.3 MW
 - New intermediate water Cherenkov detector and upgraded near detectors

Wide range of physics

- * CP violation in the lepton sector
- * Nucleon decays
- * Astrophysics
- * Potential to discover new physics

New collaborators welcome!

APPROVED



**Construction underway
Data taking in 2027**

BACKUP SLIDES



Lomonosov 2021

BACKUP SLIDES

HYPER-K COLLABORATION:

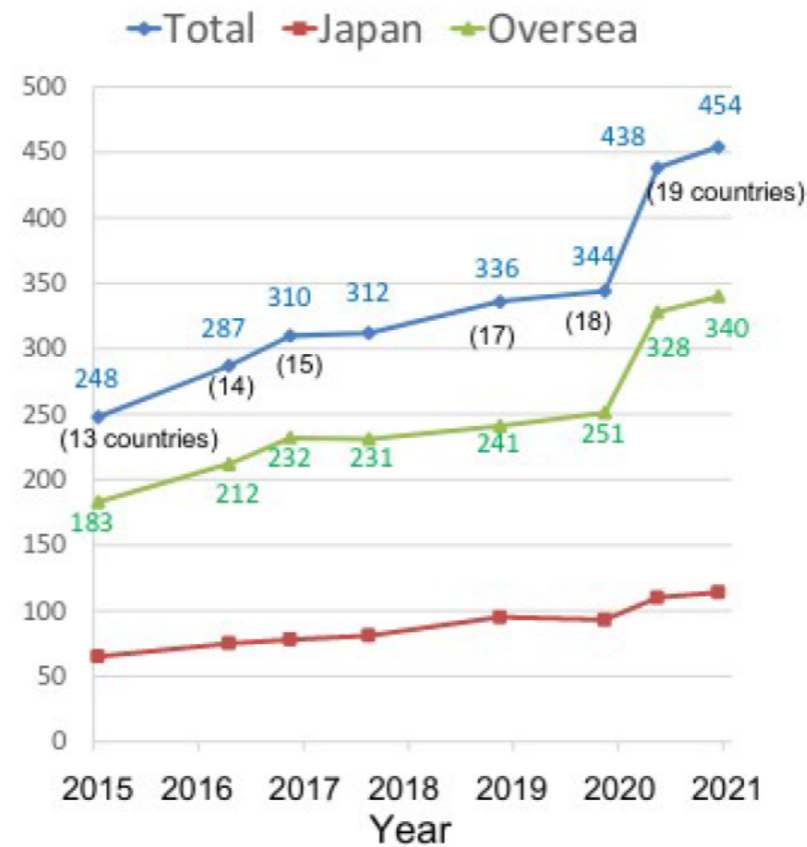
19 countries, 93 institutes, ~450 people as of May 2021, still growing

Collaborating Institutes



Europe		Asia	
Armenia	3	India	10
Czech	3	Korea	18
France	28	Japan	114
Germany	1	Americas 52 members	
Italy	53	Brazil	3
Poland	37	Canada	29
Russia	21	Mexico	11
Spain	26	USA	9
Sweden	5		
Switzerland	5		
Ukraine	4		
UK	74		

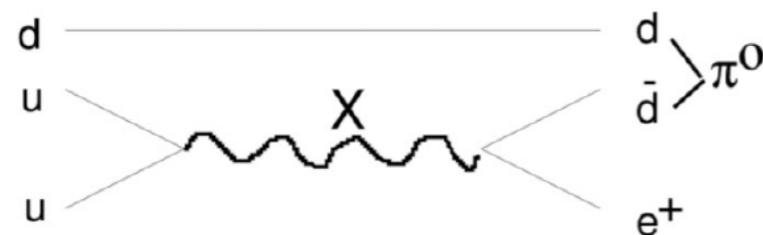
Number of Collaborators



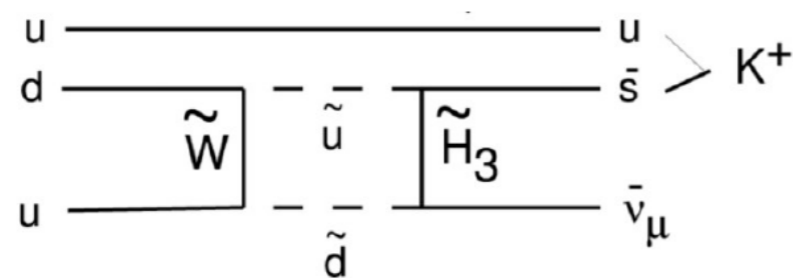
BACKUP SLIDES

Proton decay and neutrinos

$$p \rightarrow e^+ \pi^0 > 1.9 \times 10^{34} \text{ years}$$



$$p \rightarrow \nu K^+ > 0.8 \times 10^{34} \text{ years}$$



Atmospheric nu still biggest background for kaon mode

Originally proposed by Sakharov to provide baryon number violation to explain the matter-antimatter asymmetry of the universe.

Many GUT predict proton decay

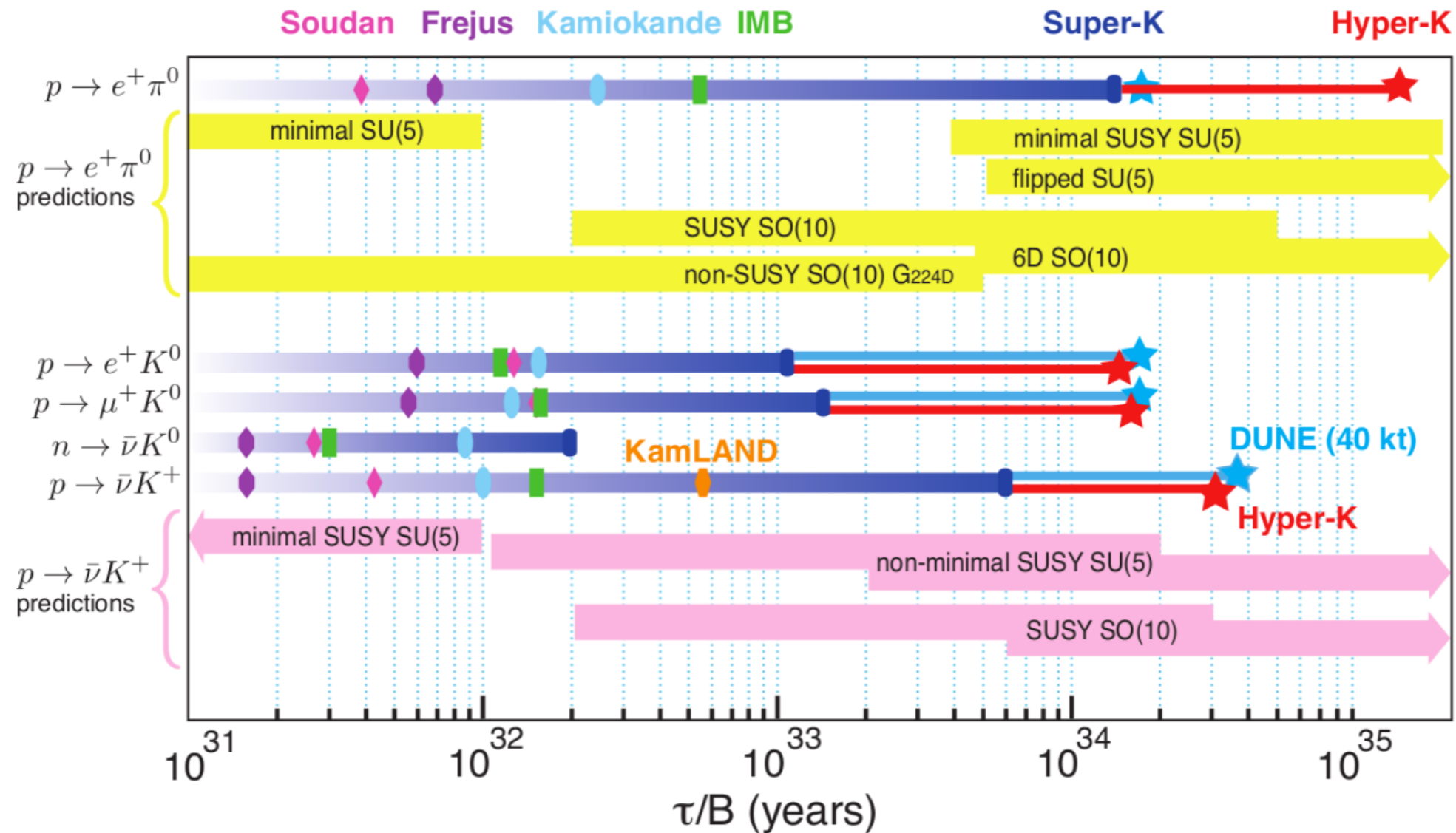
KamiokaNDE (Kamioka Nucleon Decay Experiment) I&II

- Did **not observe proton decay**
- ruled out many GUTs at the time
- observed **Supernova 1987a**
- saw hints of **neutrino oscillation**
 - solar neutrinos
 - atmospheric neutrinos

Super-K limit on proton decay $> 10^{34}$ years

BACKUP SLIDES

Proton decay



BACKUP SLIDES

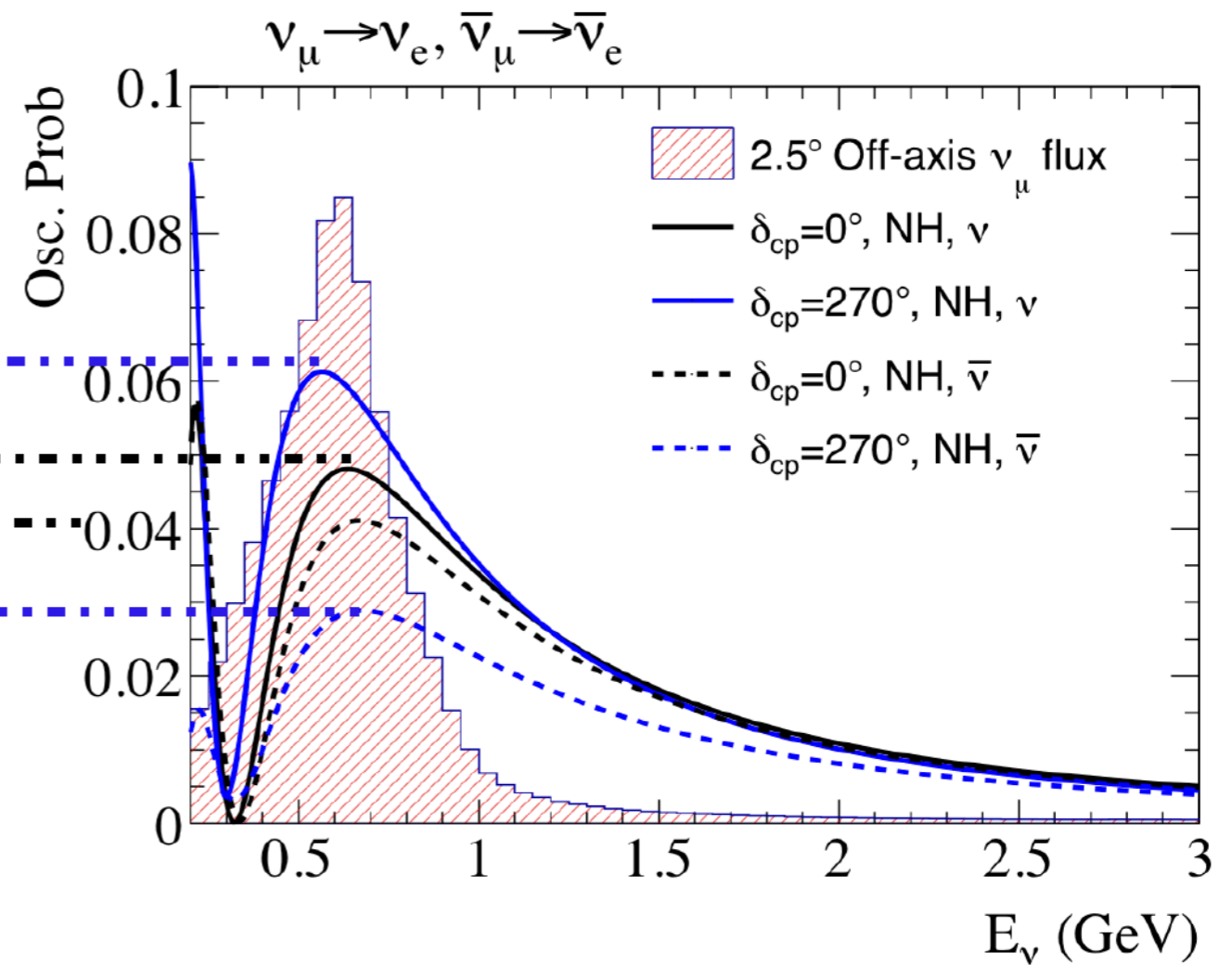
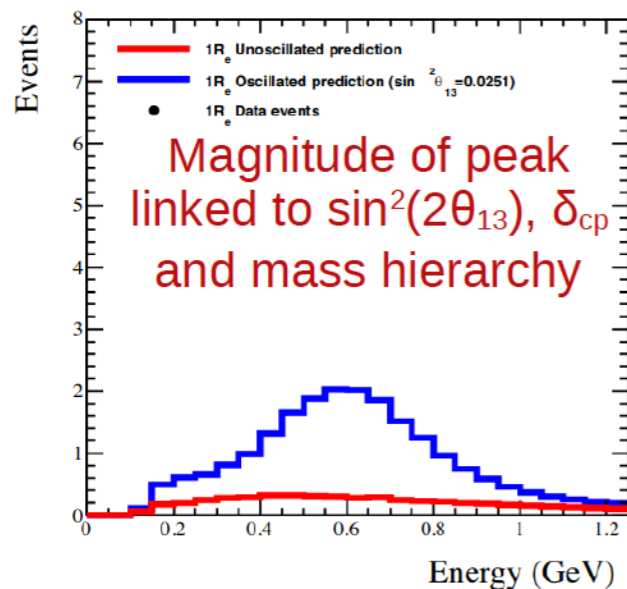
ν_e ($\bar{\nu}_e$) appearance

Oscillation peak causes peak in ν_e ($\bar{\nu}_e$) observed at SK

sensitive to $\theta_{23} < \pi/4$ or $\theta_{23} > \pi/4$

Maximum possible δ_{cp} effect ~30%

Matter effect



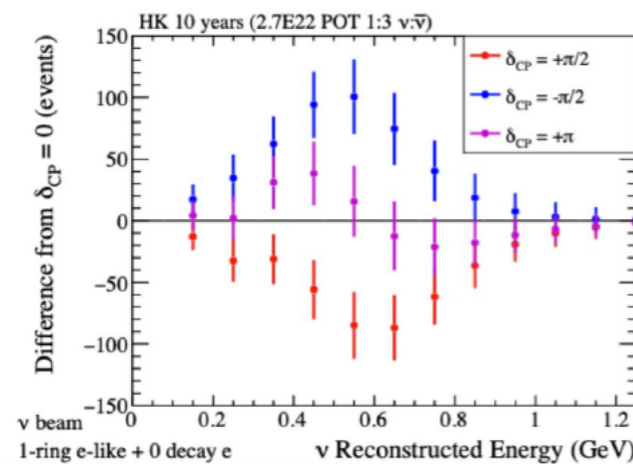
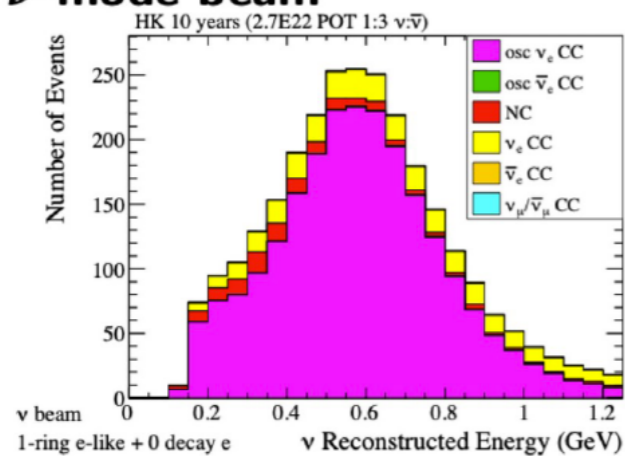
Test CP symmetry

BACKUP SLIDES

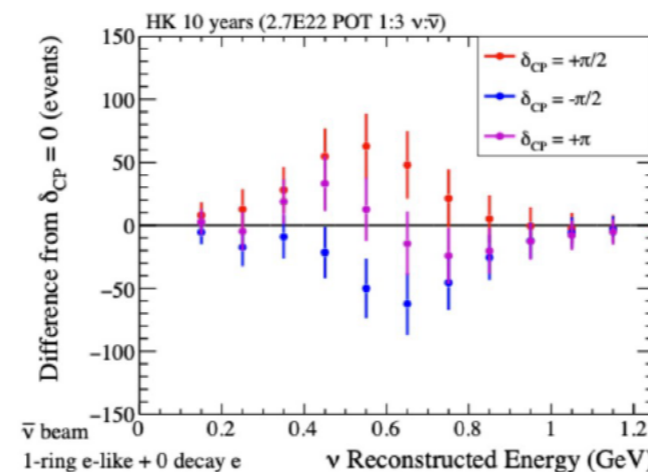
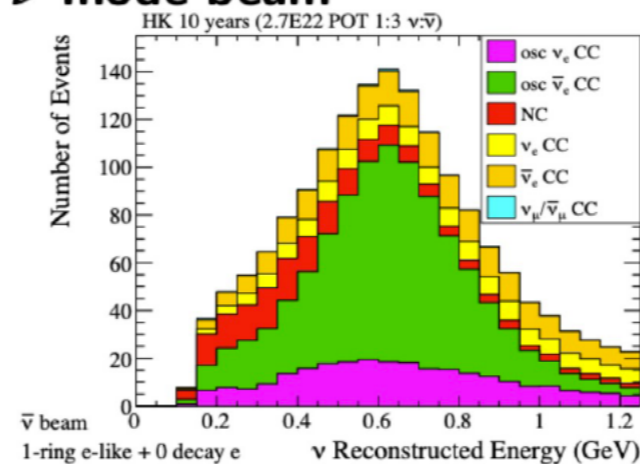
Hyper-Kamiokande long-baseline



ν -mode beam



$\bar{\nu}$ -mode beam



Predicted HK far detector event yields for 10 years of operation

$$\nu : \bar{\nu} = 1 : 3$$

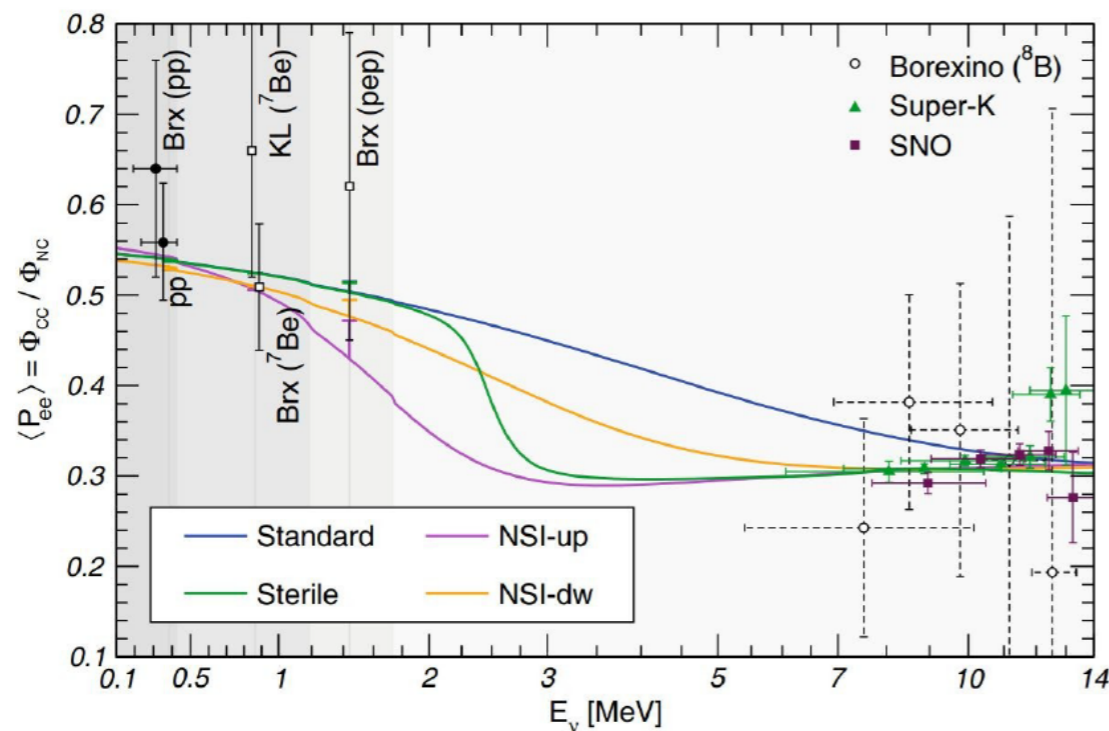
Run mode chosen to optimise deltaCP sensitivity

BACKUP SLIDES

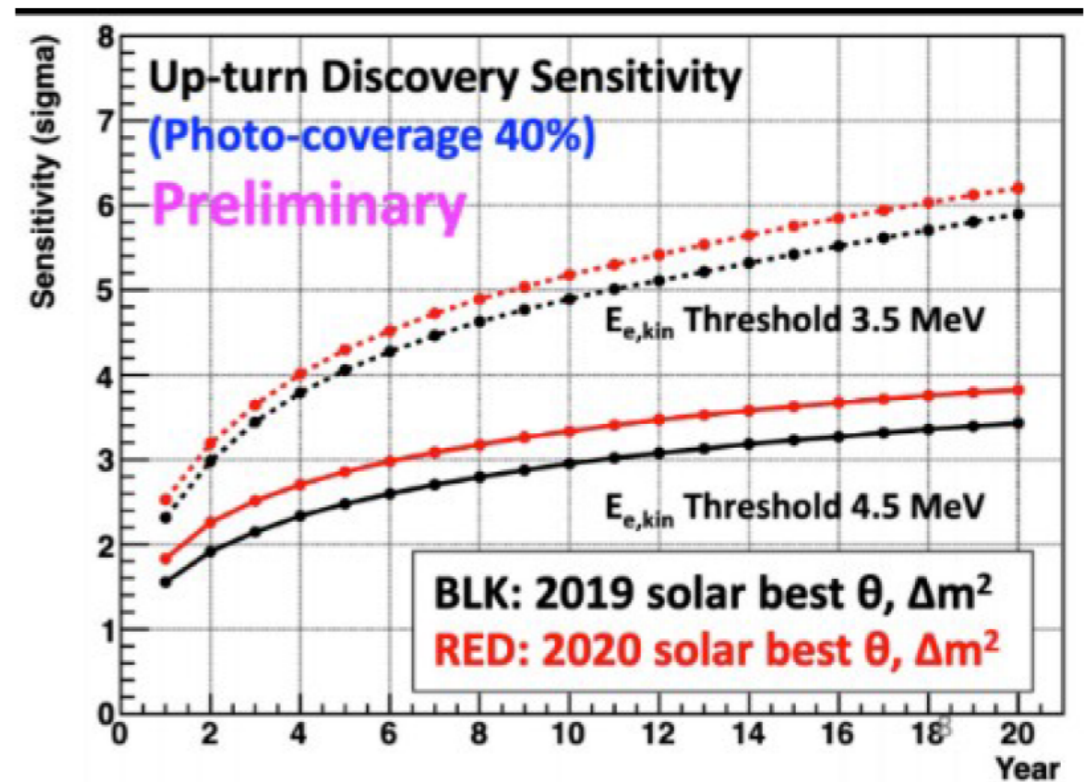
Solar Neutrinos



‘Upturn’: increase in the solar neutrino survival probability at low energy
 → transition region between matter dominated and vacuum dominated oscillations



M. Maltoni et al., Phys. Eur. Phys. J. A52, 87 (2016)

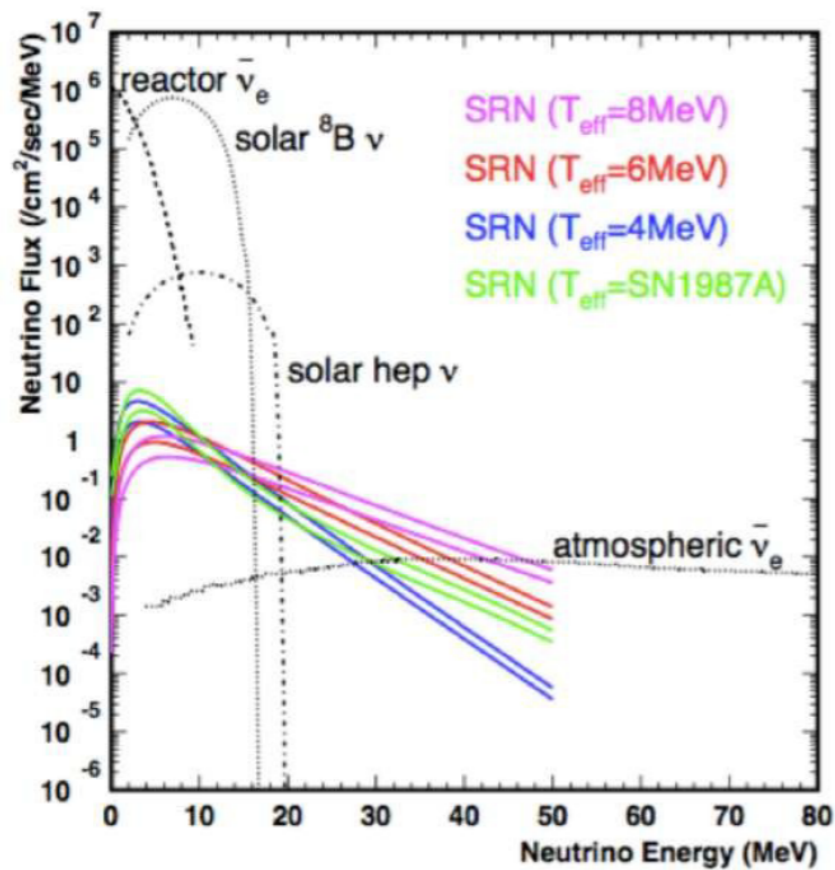


Significance of upturn detection at HK

BACKUP SLIDES

Supernova Relic Neutrinos

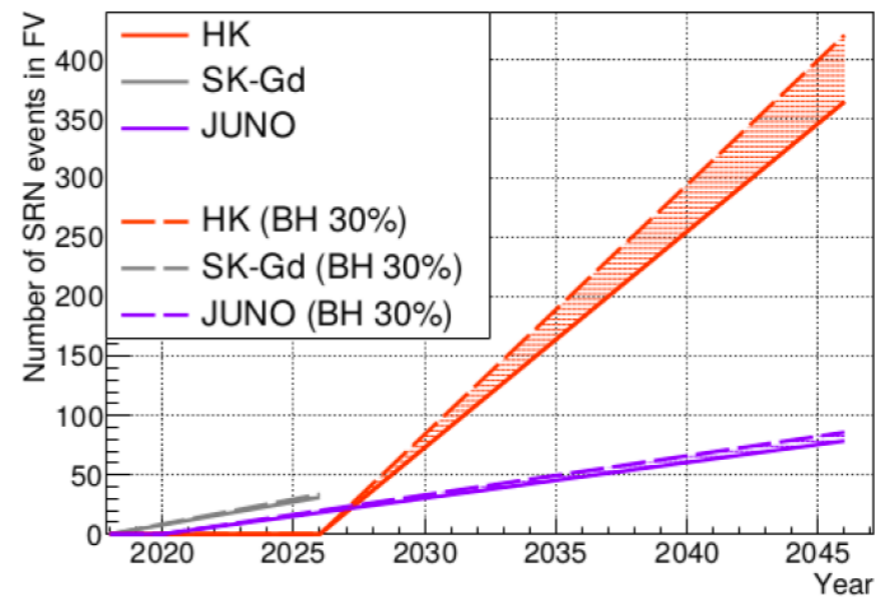
Predicted flux for different models



- * Small flux
- * Large backgrounds

→ No evidence of supernova relic neutrinos at SK yet

Predicted event numbers



Dashed line for case where 30% form black hole and emit higher energy neutrinos

BACKUP SLIDES

Supernova Neutrinos



M31 (Andromeda 6898 Galaxy)
~ 10 to 16 events expected at Hyper-K.

Large Magellanic Cloud (where SN1987A was located)
~ 2,200 to 3,600 events expected at Hyper-K

Betelgeuse (200pc)
~ 117.5 million – 180 million

BACKUP SLIDES

Supernova Neutrinos



- * Blackhole formation can be observed as a sharp drop in neutrino flux
- * Hyper-K can confirm/refute models relating to the dynamics of the explosion
(Standing Accretion Shock Instability)
- * Supernova flux is sensitive to mass ordering without too much model dependence
→ neutronization burst

BACKUP SLIDES

The Kamiokande Series



Hyper-K: Height $h = 71\text{m}$, diameter $d = 68\text{m}$
Volume $V = 258 \text{ kton}$, Fiducial Volume $FV \geq 187 \text{ kton}$

Super-K: $h = 41.4\text{m}$, $d = 39.1\text{m}$
 $V = 50\text{kton}$, $FV: 22.5 \text{ kton}$

Kamiokande

$h = 16 \text{ m}$
 $d = 15.6 \text{ m}$
 $V = 3 \text{ kton}$
 $FV = 0.68 \text{ kton}$

KamiokaNDE

3 kton

Super-Kamiokande

50 kton

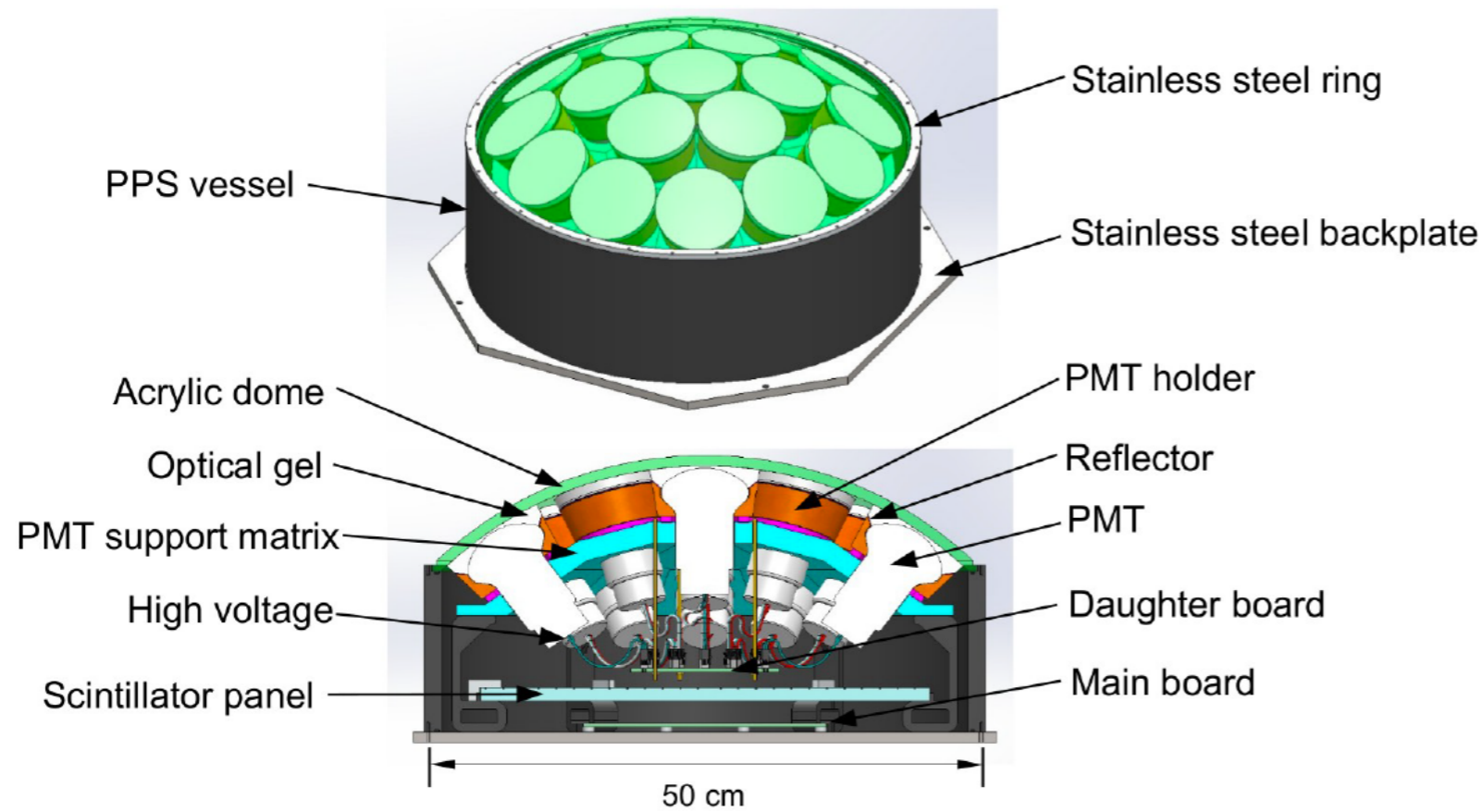
Hyper-Kamiokande

258 kton



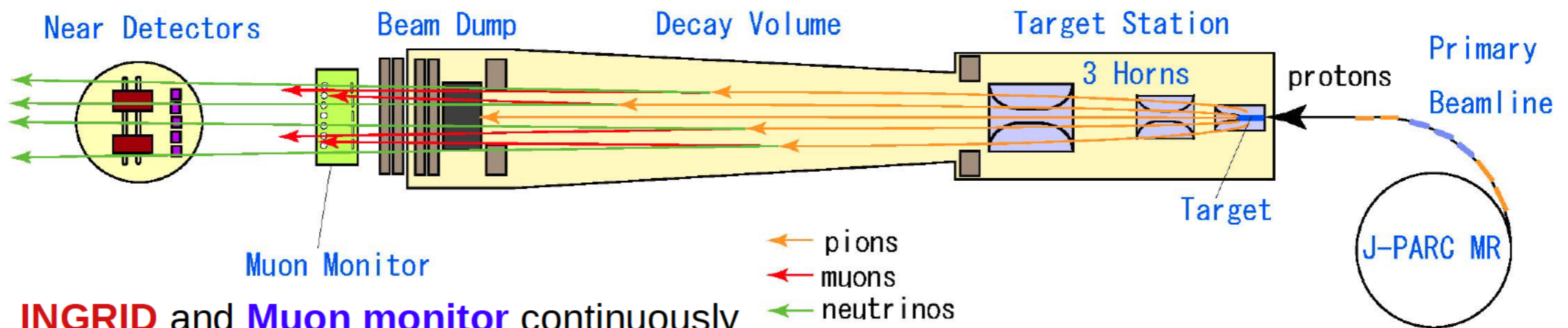
BACKUP SLIDES

Multi-PMT (mPMT)



BACKUP SLIDES

Neutrino beam



INGRID and **Muon monitor** continuously measure beam rate and direction

- * **30GeV protons** → **graphite** target → charged **hadrons**
- * **charge selection** and focusing of hadrons with **3 electromagnetic horns**
- * **hadrons decay to ν or $\bar{\nu}$** (depending on charge of hadron)

Dominant systematic error due to hadron interaction modelling

- Constrained using NA61/SHINE replica target measurements
- In future flux uncertainty will be reduced by the EMPHATIC experiment

BACKUP SLIDES

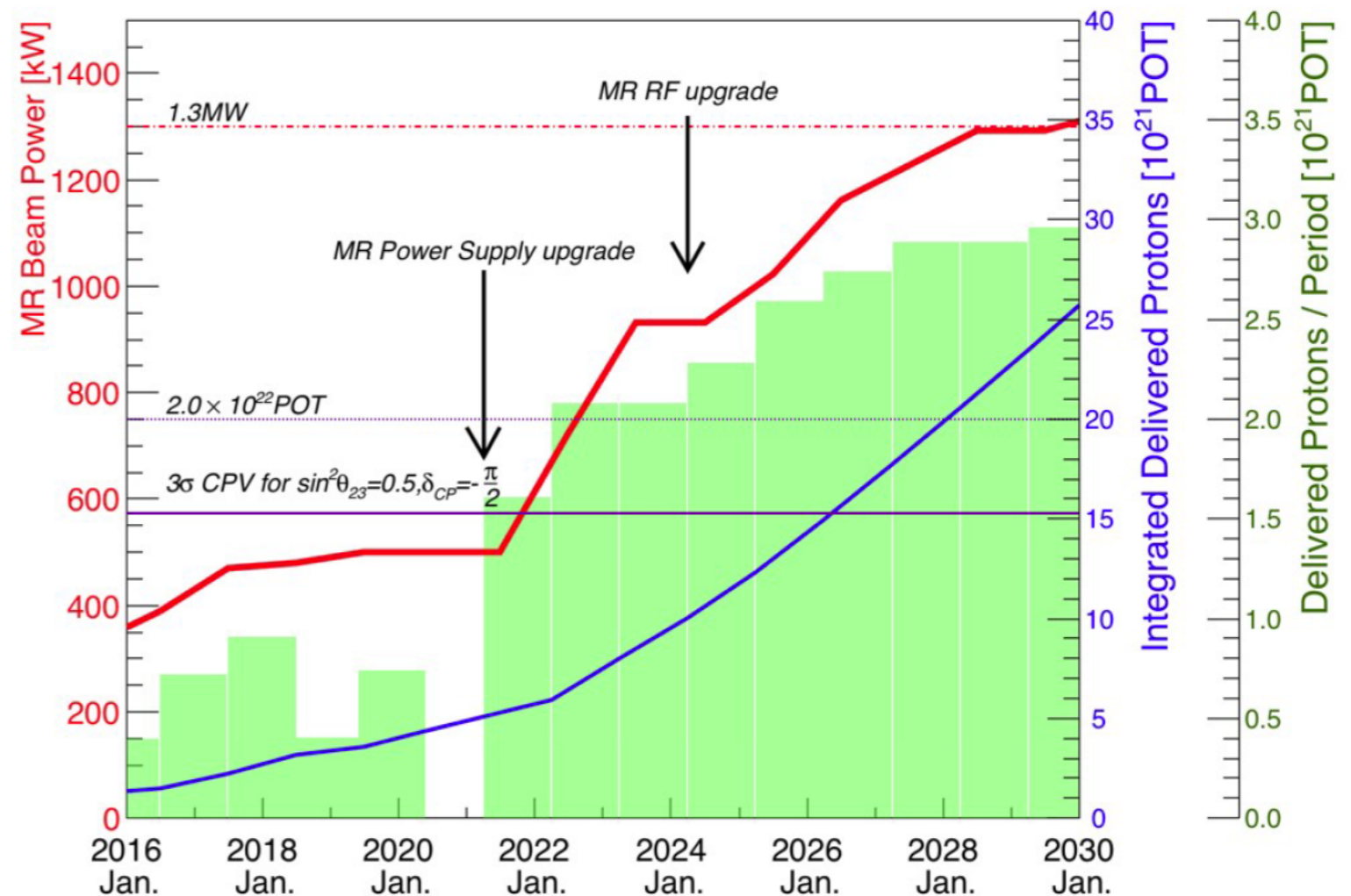
T2K/HK Beam upgrade



* Beam currently capable of 450-500kW stable running

* Beam line upgrade in 2021
- Nd280 upgrade will happen at the same time

* target power: 1.3MW

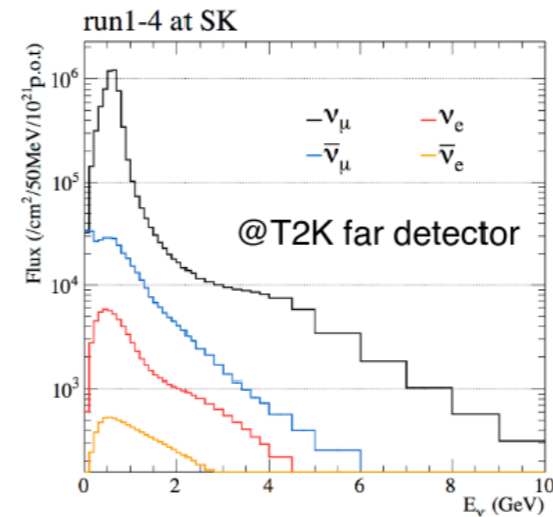


BACKUP SLIDES

J-PARC neutrino beam flux and its error

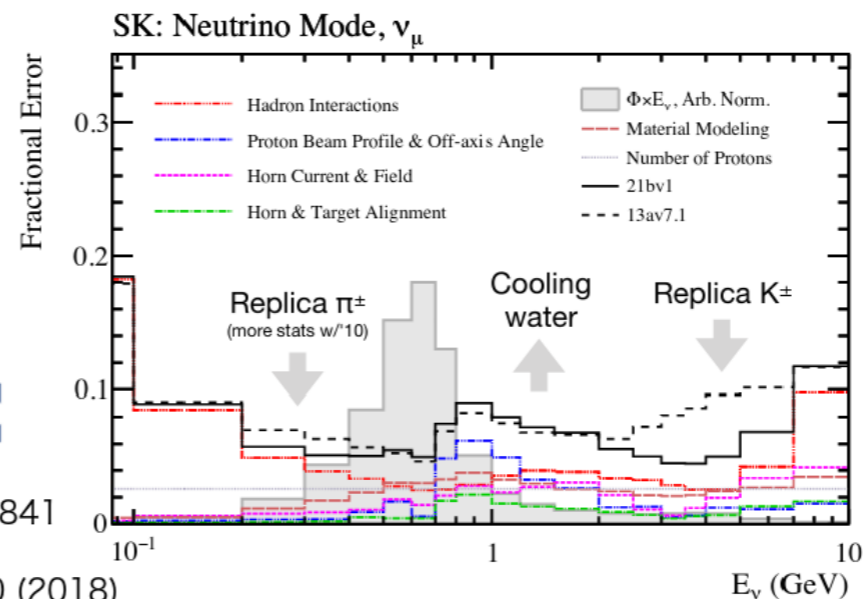
ν flux is predicted based on hadron production and in-situ proton beam measurements

- ❖ Recently flux error was improved with NA61/SHINE replica 2010 data : **~5% error**
- ❖ Further reduction of flux systematic errors, several activities are underway



Hadron production is still largest error source

New measurements at NA61/SHINE, EMPHATIC are underway to reduce the remaining flux error



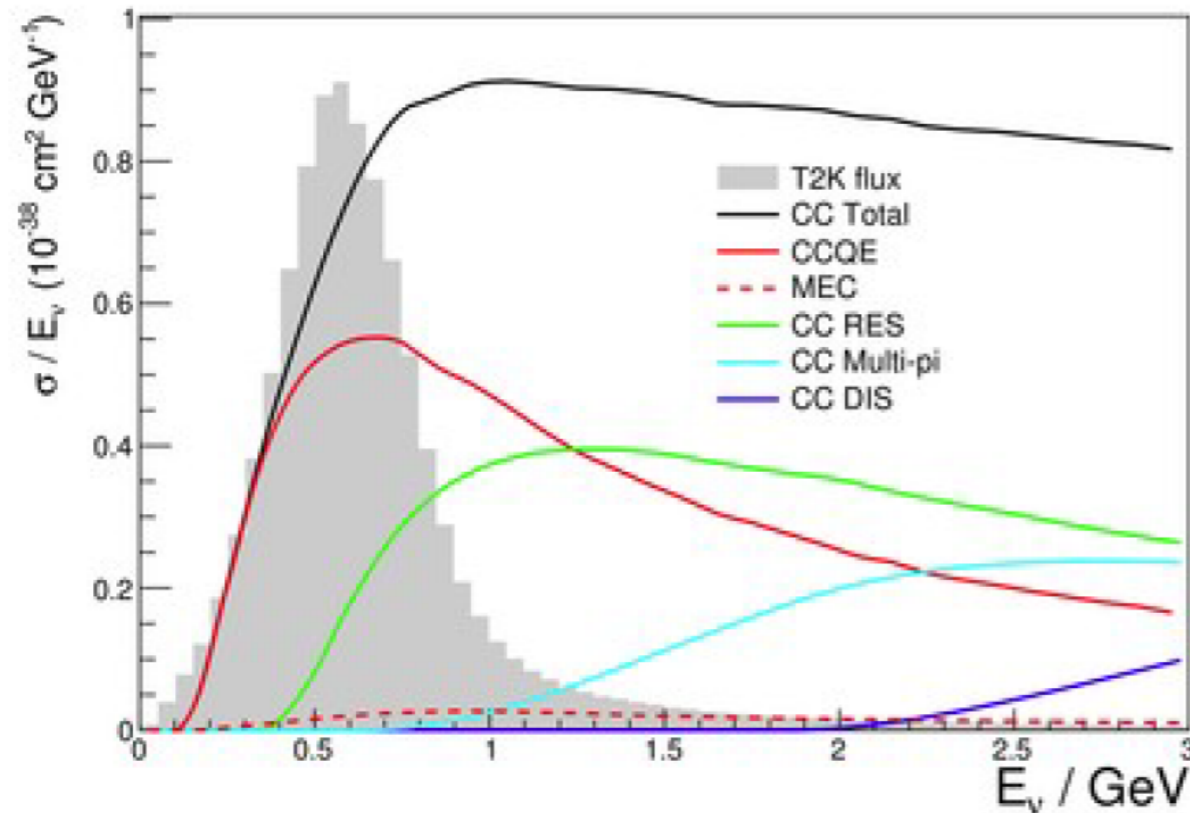
arXiv:1912.08841

CERN-SPSC-2018-008, SPSC-P-330-ADD-10 (2018)

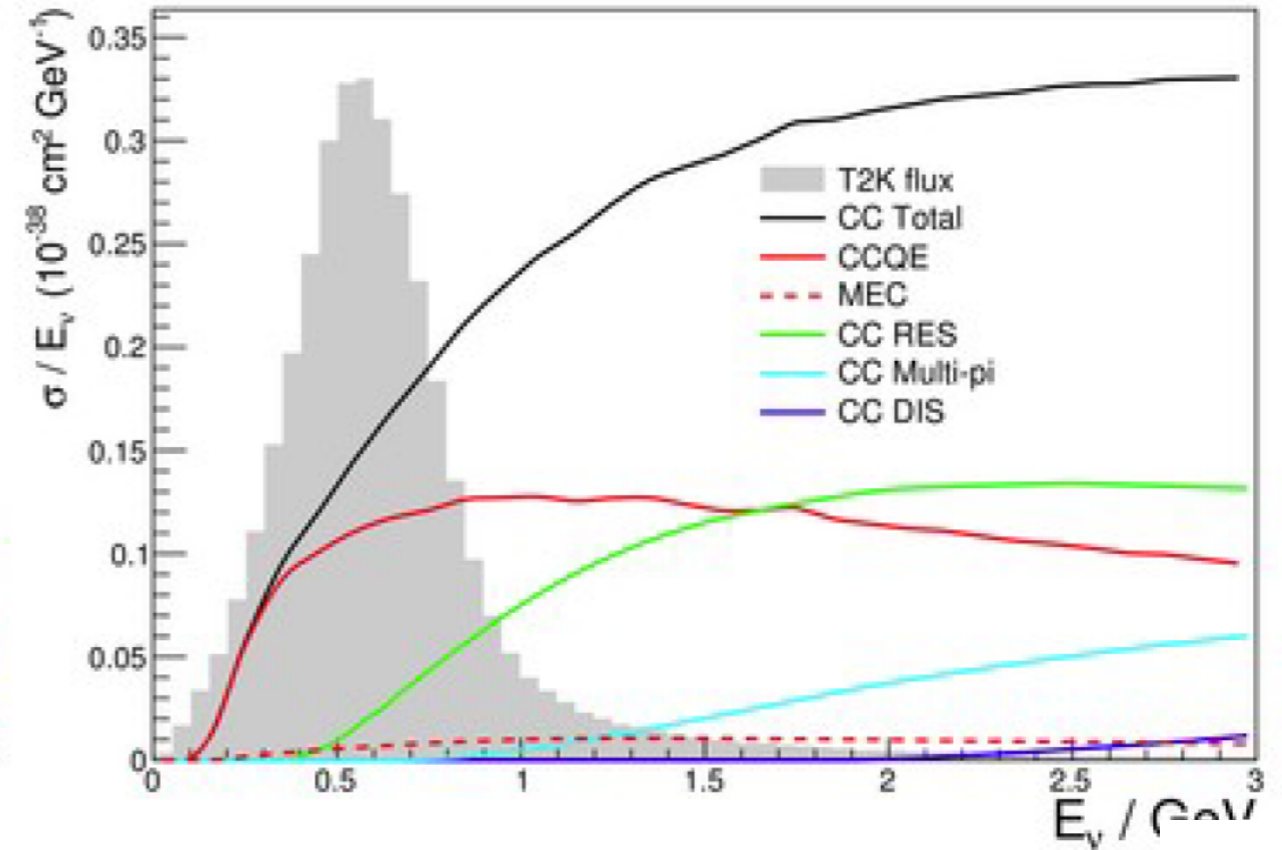
BACKUP SLIDES

Neutrino interaction cross sections and T2K/HK flux

ν

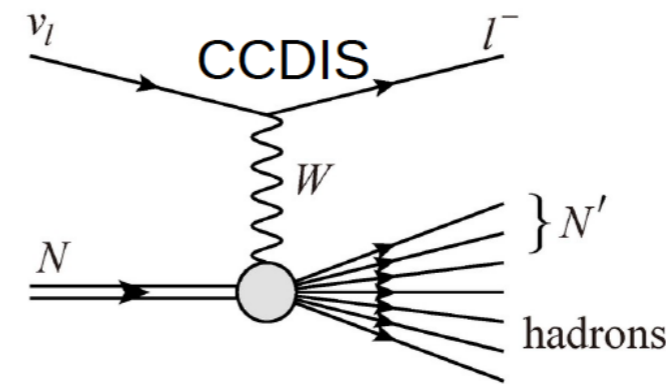
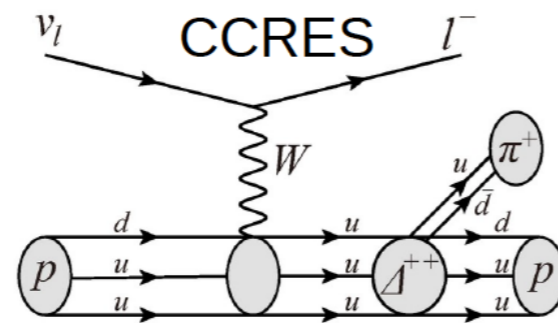
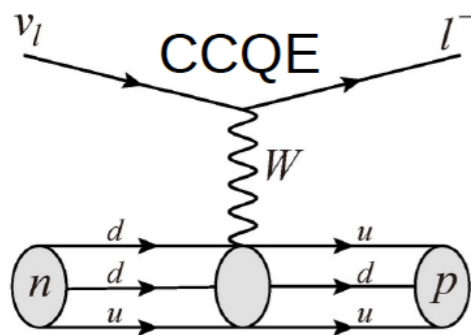


$\bar{\nu}$

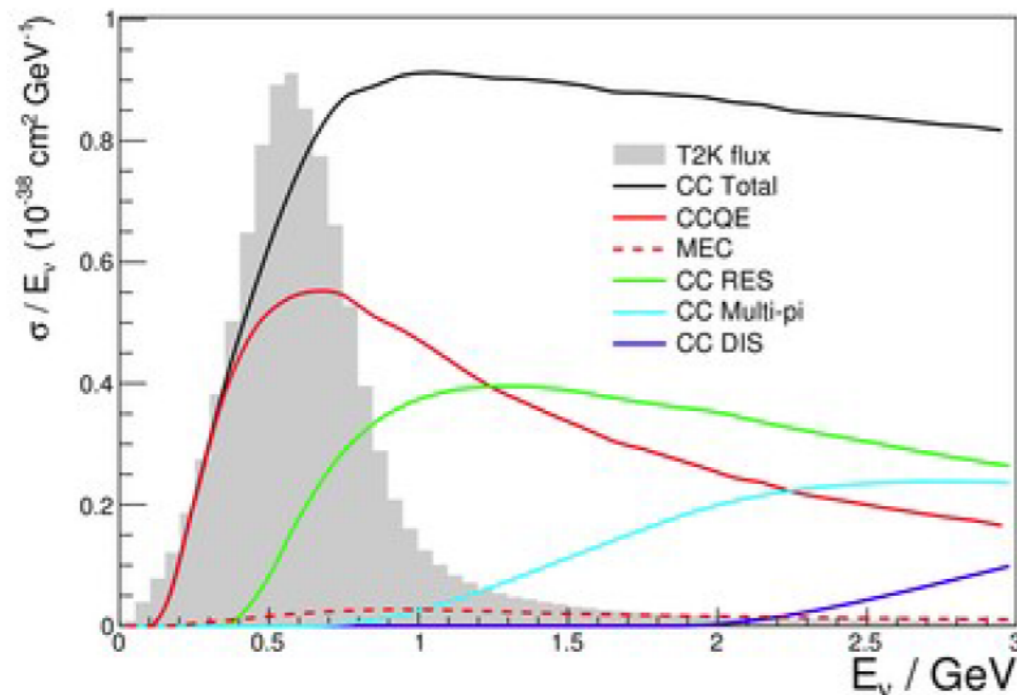


BACKUP SLIDES

Neutrino interactions



NC interactions also important
e.g. NC π^0 , NC1 γ
→ background



Interactions occur with nucleons bound inside a nucleus

→ **Nuclear effects!!**

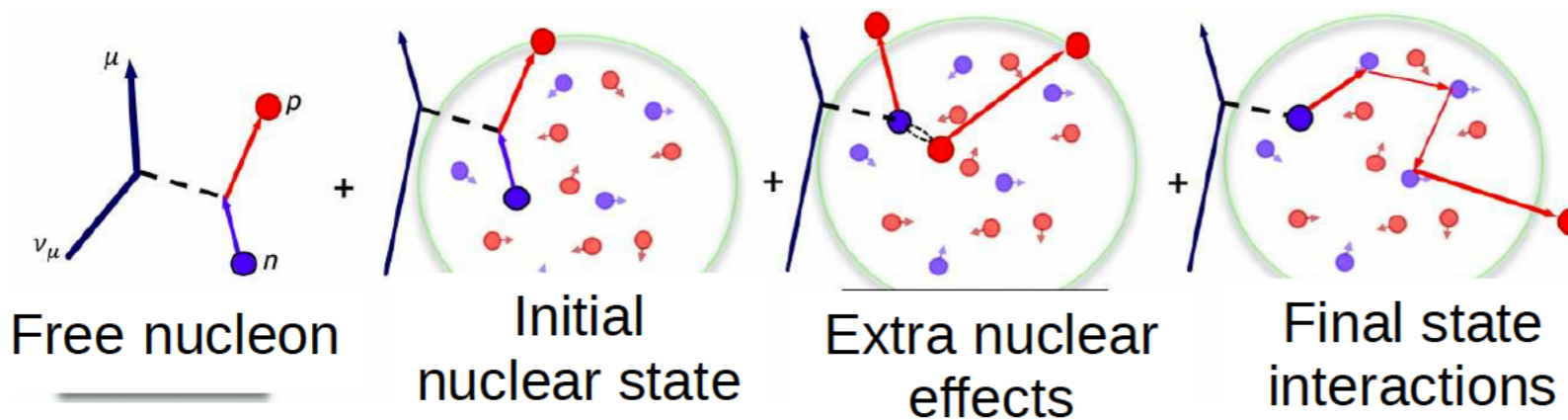
We only measure particles that exit the nucleus

→ lose information about the initial interaction

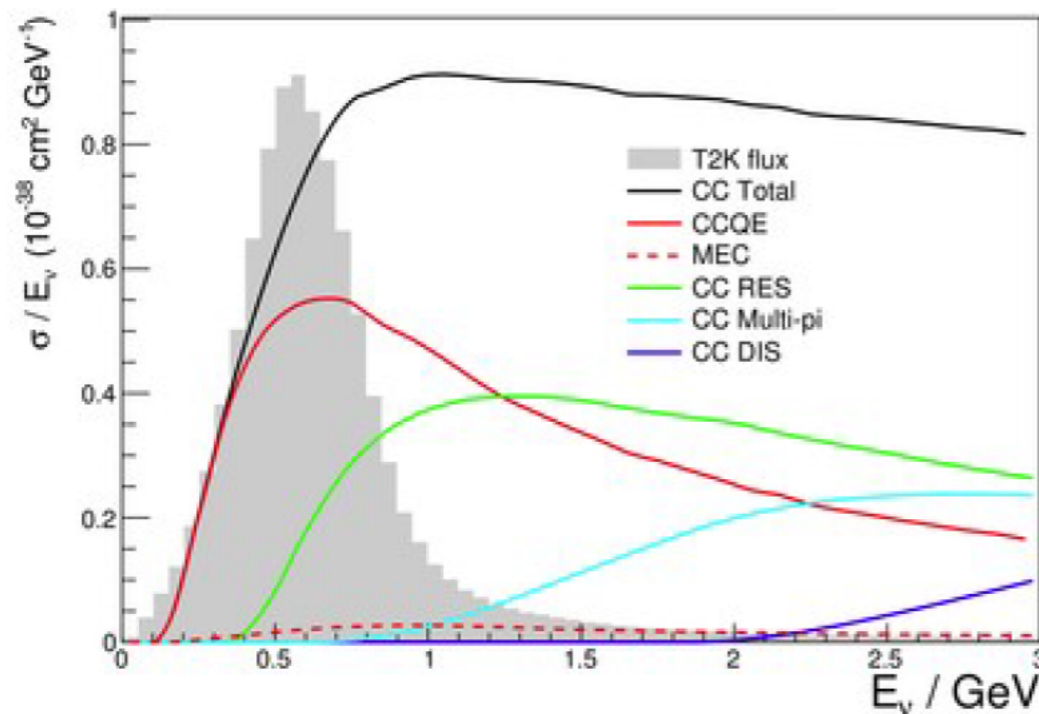
→ can create a bias in energy reconstruction

BACKUP SLIDES

Neutrino interactions



Interaction modes and Nuclear models tuned to external data



Interactions occur with nucleons bound inside a nucleus

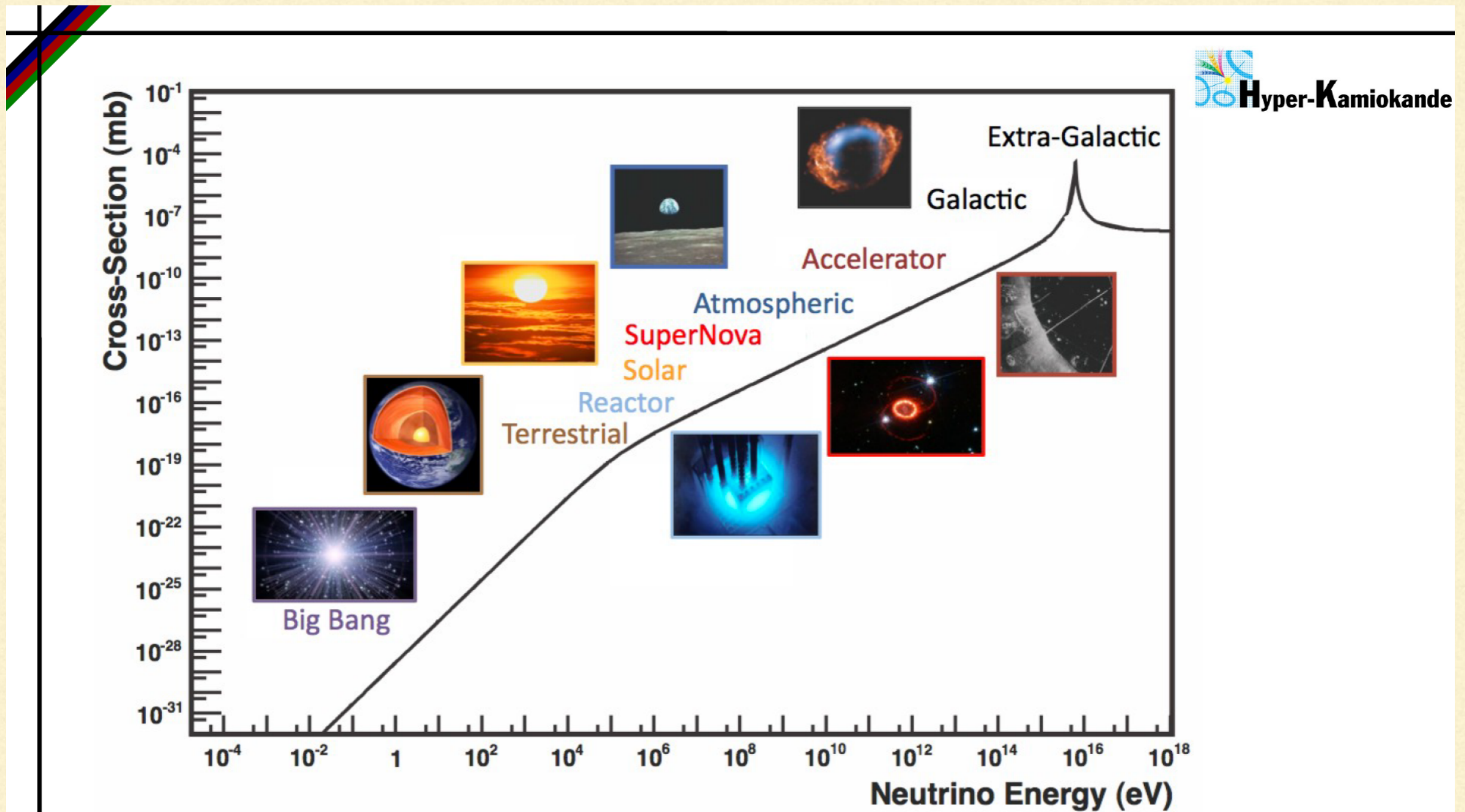
→ **Nuclear effects!!**

We only measure particles that exit the nucleus

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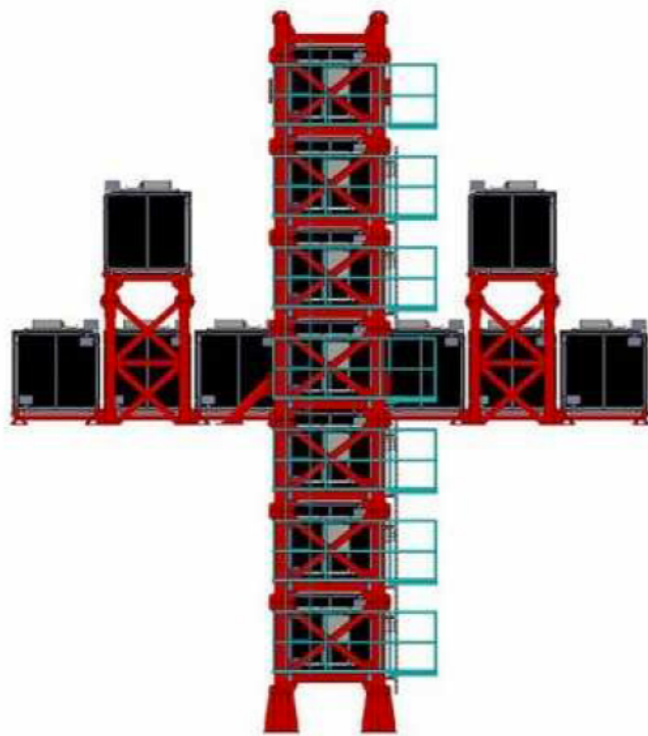
BACKUP SLIDES



BACKUP SLIDES

Near Detectors

280m from the ν ($\bar{\nu}$) source



INGRID

- On-axis, scintillator and iron
- monitors beam direction, intensity and stability

BACKUP SLIDES

Near Detectors

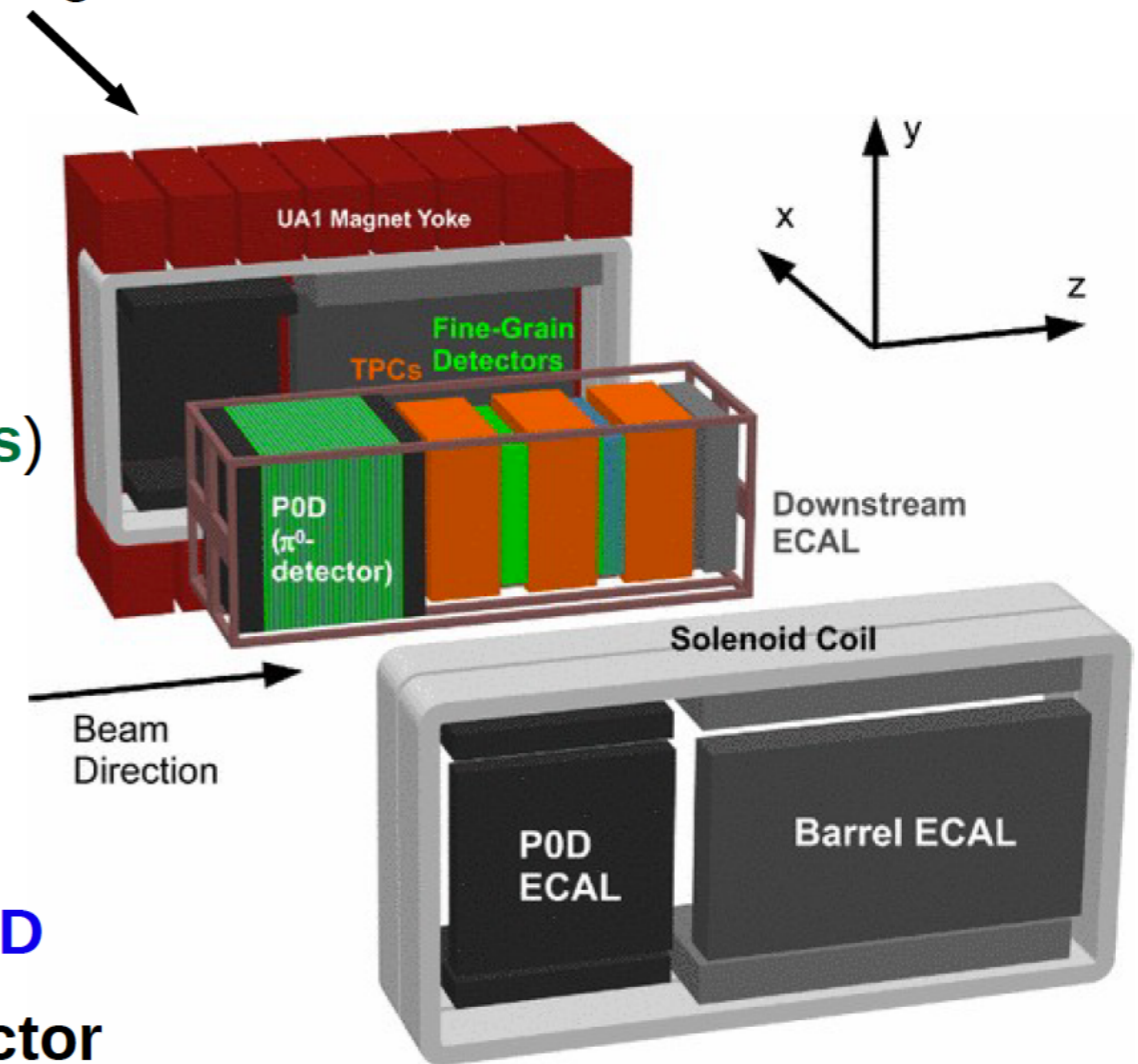
280m from the ν ($\bar{\nu}$) source

ND280

Same off-axis angle as SK

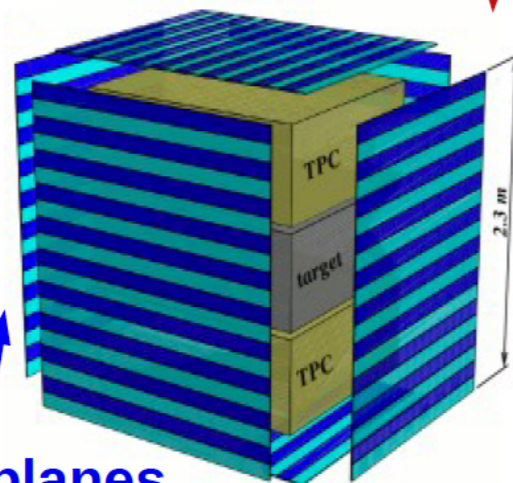
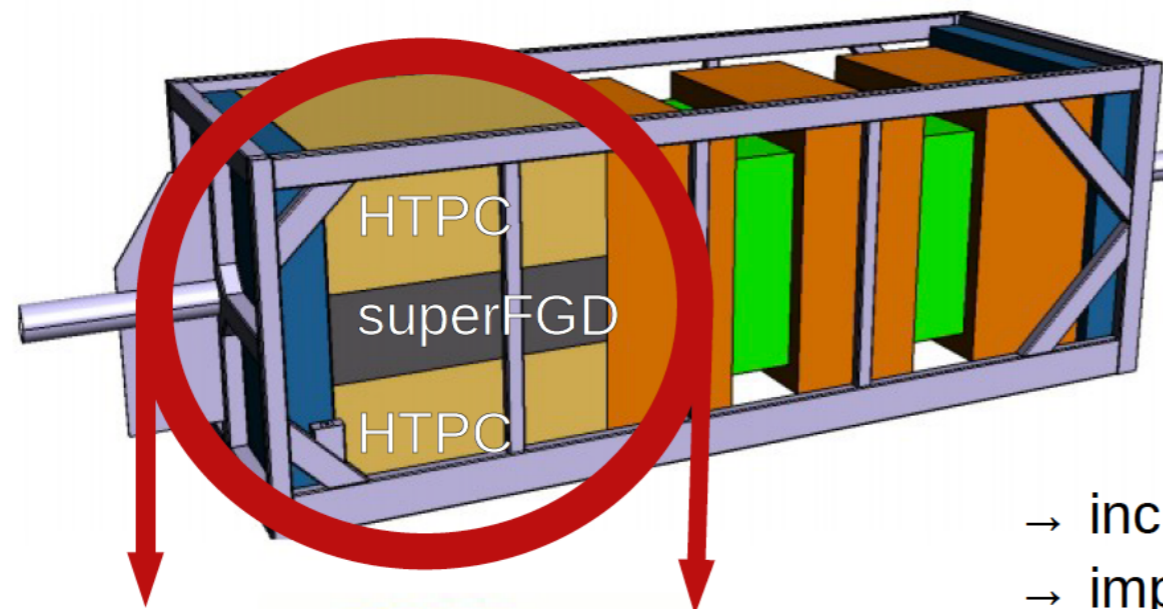
- Active target mass \rightarrow 2 x scintillators (**FGDs**)
 \rightarrow vertex reconstruction
- 3 Time projection chambers (**TPC**)
 \rightarrow **momentum** reconstruction
 \rightarrow **charge** identification
 \rightarrow Particle identification (**PID**)
- Electromagnetic calorimeters (**Ecal**) \rightarrow **PID**
- π^0 detector and side muon range detector

Magnetised



BACKUP SLIDES

ND280 upgrade (2021)



6 ToF planes

Pi0 detector is being replaced by

* SuperFGD

- higher granularity, 3D readout

* Horizontal TPCs (HTPCs)

* Time of Flight (ToF) planes

- increases active target **mass** for oscillation analysis
- improved **angular acceptance**
- able to reconstruct **low energy short tracks**
 - improved hadronic information
 - better $\gamma \rightarrow e^+ e^-$ identification

Reduce systematic uncertainty to 4%

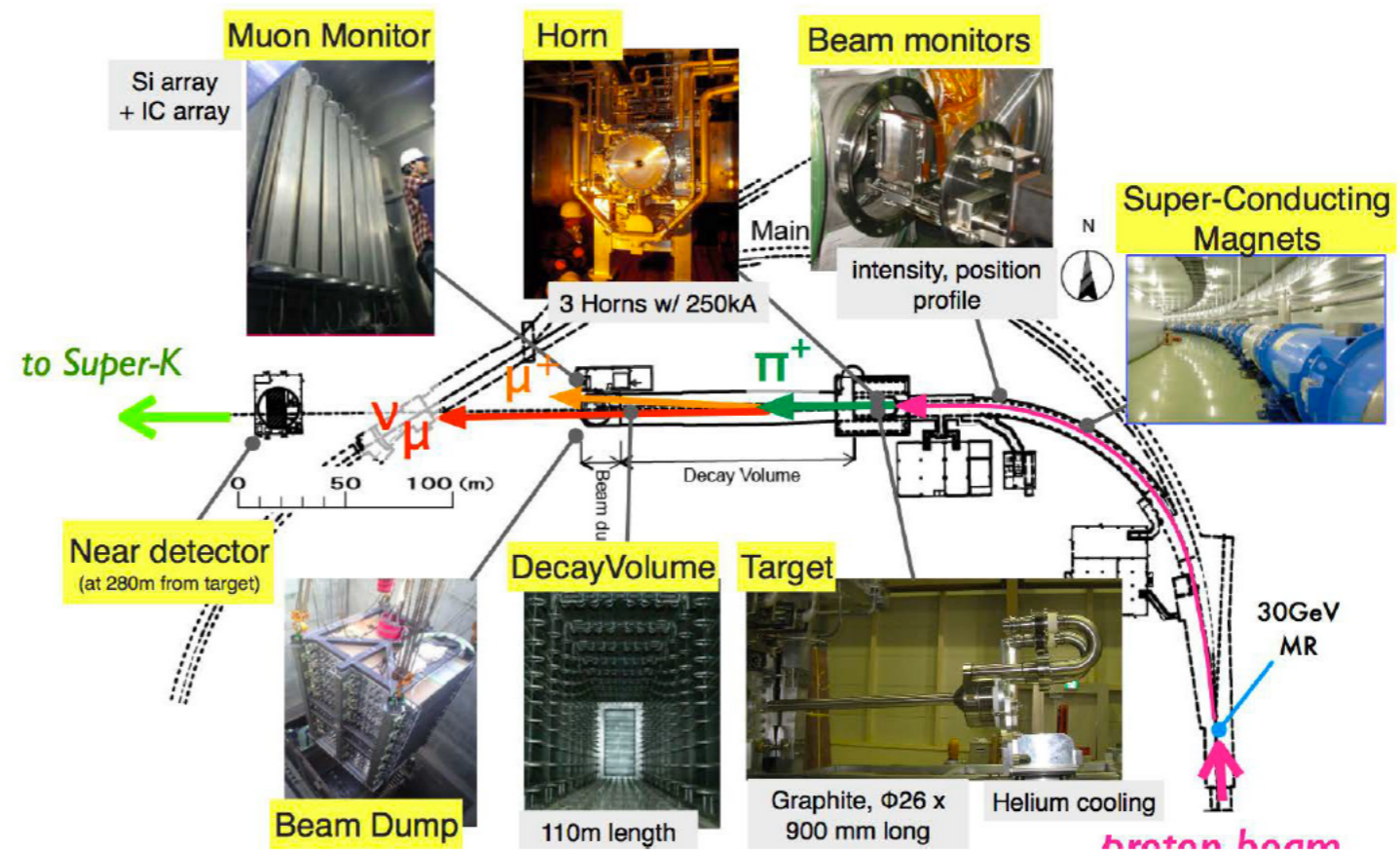
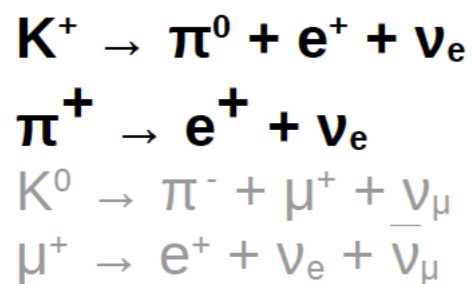
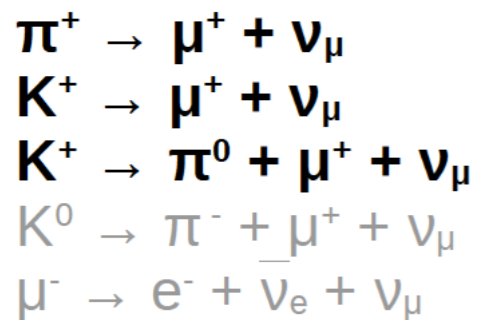
- 3σ exclusion of CP conservation for 36% of the δ_{cp} phase space (if mass hierarchy is known)

BACKUP SLIDES

The Beam

Major neutrino-producing decay modes in the decay volume:

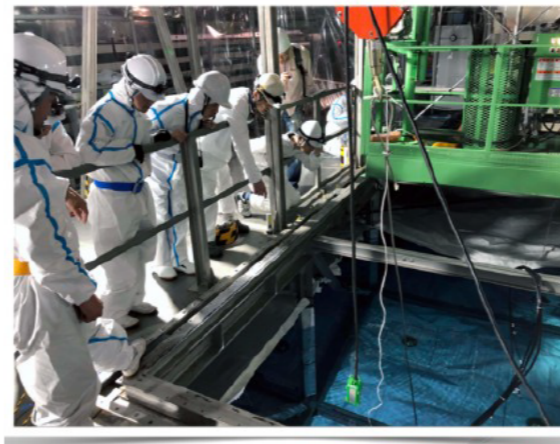
For a neutrino beam



BACKUP SLIDES

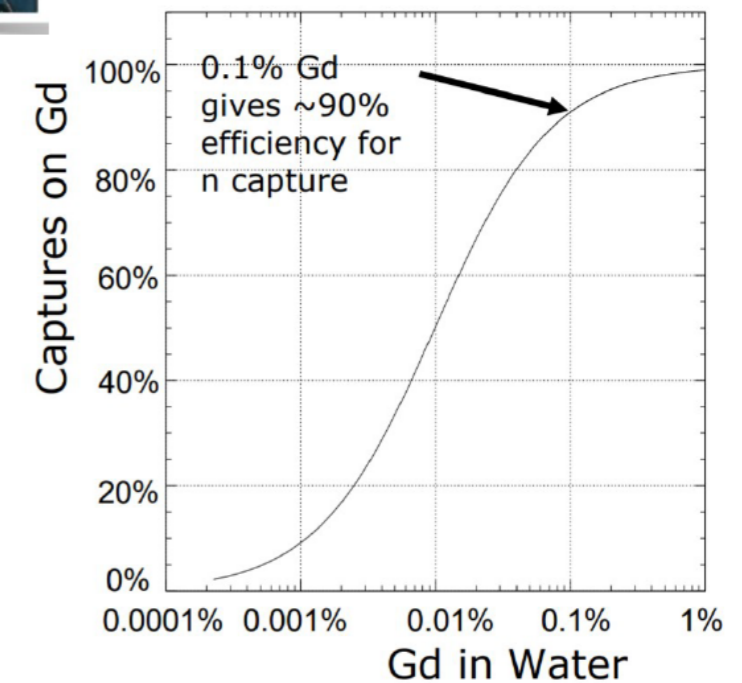
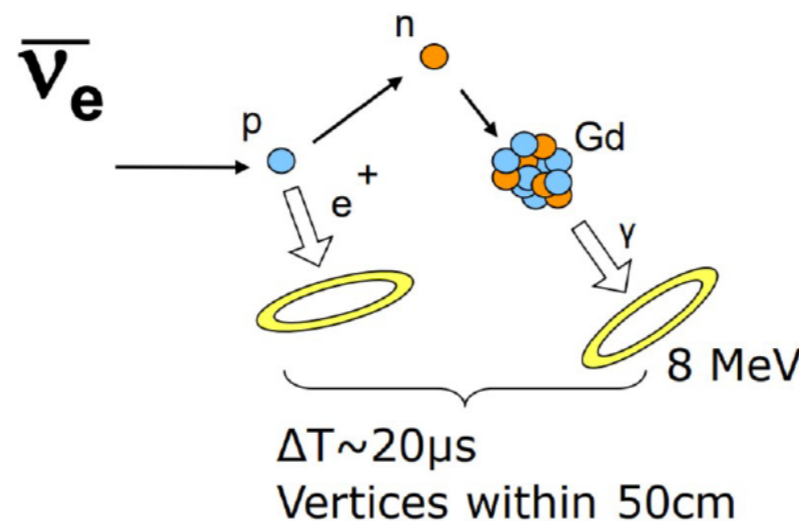
T2K II: SK upgrade

- * SK repairs performed in 2018
 - detector drained and cleaned
 - reinforcement of water sealing
 - improved tank piping
 - PMTs replaced



- * Plan to add **Gadolinium** to the water
 - 0.01% next year
 - increase to 0.1% eventually

→ **Better ν / $\bar{\nu}$ separation**



BACKUP SLIDES

Neutrino Oscillations

Flavour eigenstate: Interact

Mass eigenstate: Propagate

} Neutrino oscillation
 → mass states do not align with flavour states
 → non-zero masses

Oscillations governed by PMNS flavour-mass mixing matrix, U

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Atmospheric and
 accelerator
 $\theta_{23} \sim 45^\circ$
 $|\Delta m_{32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$

Reactor and accelerator
 $\theta_{13} \sim 8^\circ$
 Accelerator only $\delta_{CP} = ??$

Solar and
 reactor
 $\theta_{12} \sim 34^\circ$
 $\Delta m_{12}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$$

Flavour
 states

Mass
 states

$$c_{ij} = \cos(\theta_{ij}), \quad s_{ij} = \sin(\theta_{ij})$$

$$\Delta m_{ij}^2 = m_i^2 - m_j^2$$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \Re(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right) + 2 \sum_{i>j} \Im(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin\left(\Delta m_{ij}^2 \frac{L}{2E}\right)$$

→ **Amplitude** of oscillation: **mixing angles and phase**

→ **Distance** of oscillation: **squared mass differences and Energy**

BACKUP SLIDES

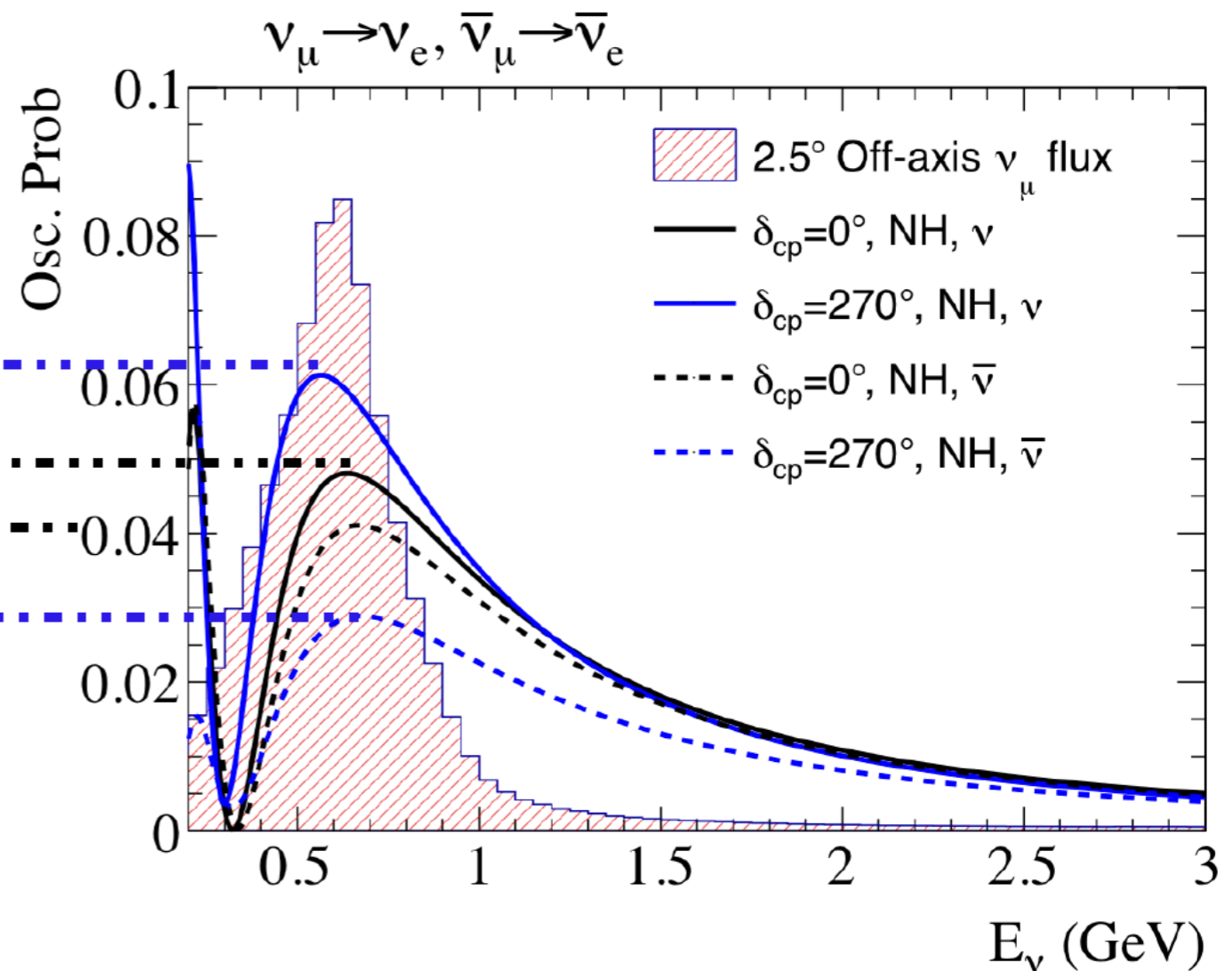
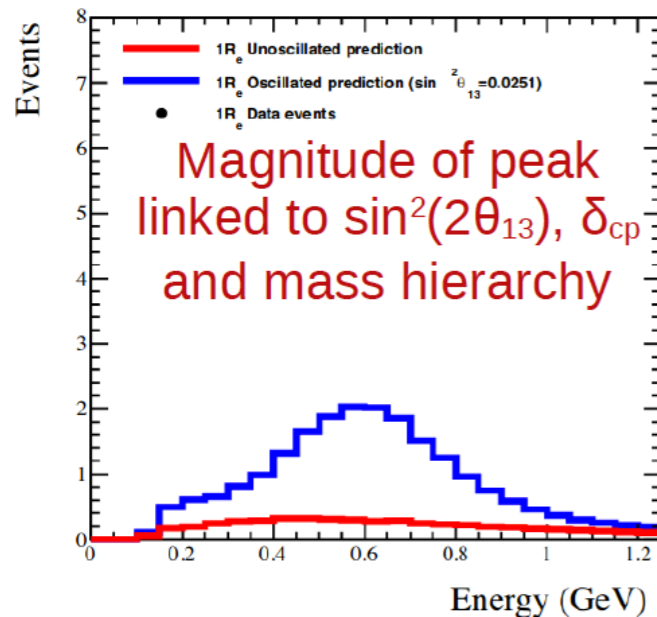
ν_e ($\bar{\nu}_e$) appearance

Oscillation peak causes peak in ν_e ($\bar{\nu}_e$) observed at SK

sensitive to $\theta_{23} < \pi/4$ or $\theta_{23} > \pi/4$

Maximum possible δ_{cp} effect ~30%

Matter effect



Test CP symmetry

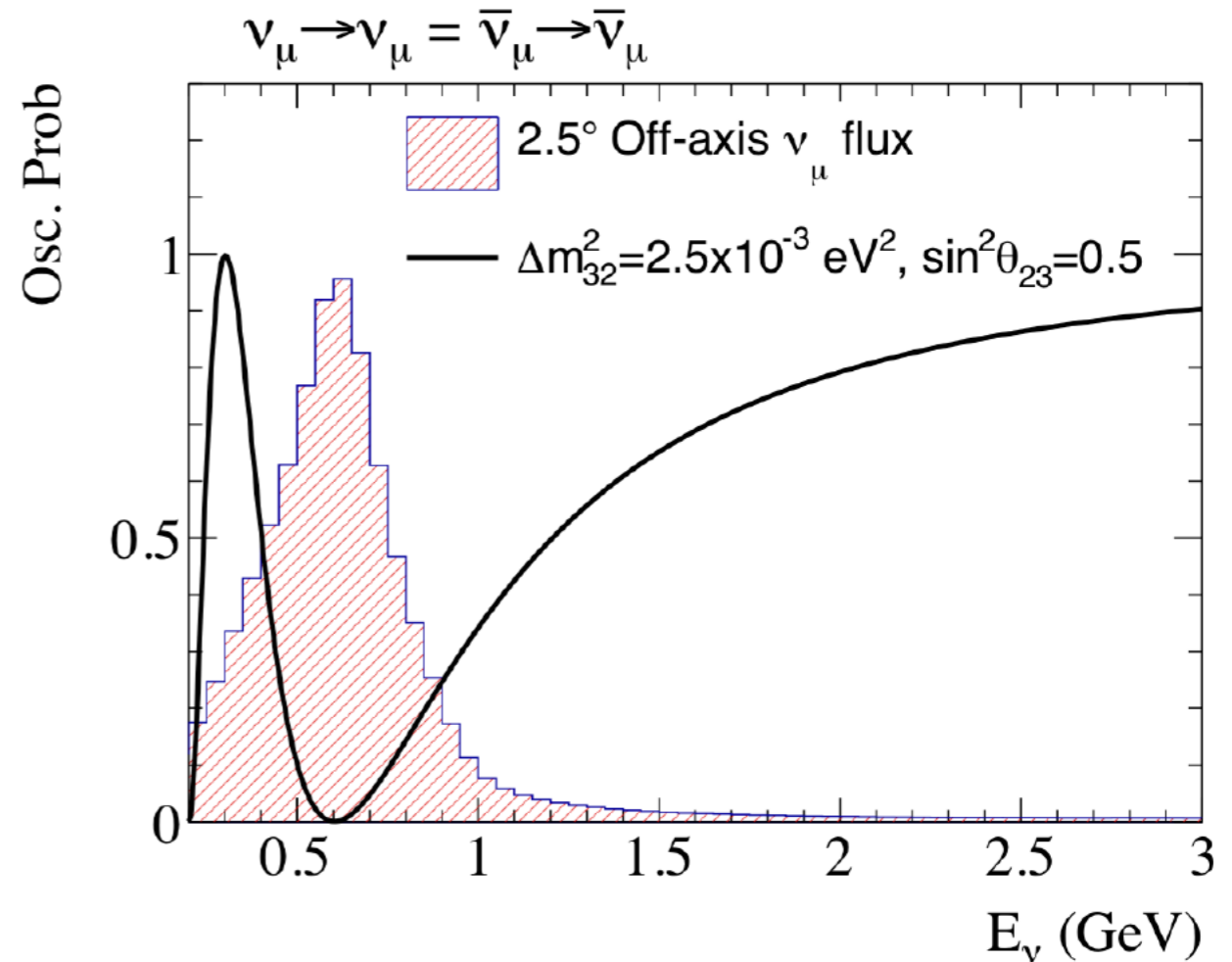
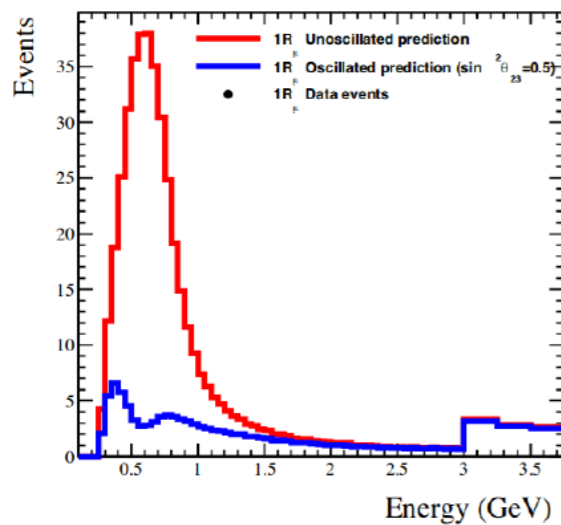
BACKUP SLIDES

ν_μ ($\bar{\nu}_\mu$) disappearance

Probability minimum causes a dip in the number of ν_μ observed at SK

Depth of dip – $\sin^2(\theta_{23})$
Energy of dip – $|\Delta m_{32}^2|$ ($|\Delta m_{13}^2|$)

Hard to distinguish mass ordering



Test CPT symmetry